

Simple Topographic Parameter Reveals the Along-Trench Distribution of Frictional Properties on a Shallow Plate Boundary Fault

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Full paper

Keywords: Subduction zone, Japan Trench, Critical taper model, Frictional variation, Accretionary wedge

Posted Date: October 13th, 2021

DOI: <https://doi.org/10.21203/rs.3.rs-948355/v1>

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Version of Record: A version of this preprint was published at Earth, Planets and Space on April 21st, 2022. See the published version at <https://doi.org/10.1186/s40623-022-01621-6>.

1 **Title page:**

2 **Title: Simple topographic parameter reveals the along-trench distribution of**
3 **frictional properties on a shallow plate boundary fault**

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17

18 **Abstract**

19 The critical taper model of a sedimentary wedge best describes the first-order
20 mechanics of a subduction zone wedge. The tapered wedge geometry, which is
21 conventionally defined by two parameters, the slope angle and the basal dip angle, is
22 responsible for the strength of a megathrust. By applying this theoretical model to
23 subduction zones, fault frictional properties and earthquake occurrences can be
24 compared among subduction zones, and within a single subduction zone, the spatial
25 distribution or temporal change of fault strength can be investigated. The slope angle
26 can be accurately estimated from bathymetry data, but the basal dip angle must be
27 inferred from the subsurface structure, and it requires highly accurate depth-converted
28 seismic reflection profiles. Thus, application of the critical taper model is often limited
29 by a lack of a sufficient number of highly accurate profiles, and the spatial distribution
30 of frictional coefficients must be inferred from relatively few data, generally less than a
31 dozen points. To improve this situation, we revisited the theoretical formula of the
32 critical taper model. We found that the effect of the décollement dip angle β on the
33 critical taper model of a sedimentary wedge is negligible when the pore fluid pressure

34 ratio is high or internal friction is small, conditions which are met in many subduction
35 zones. Therefore, this finding allows frictional variation to be approximated by using
36 only the slope angle variation obtained from the bathymetry. We applied this
37 approximation to the Japan Trench as an example of this approximation, and were able
38 to estimate the friction coefficient distribution on the shallow plate boundary fault from
39 71 data points. We found that the area where the friction coefficient was smaller than
40 the mean corresponded to the segment where a large coseismic shallow rupture
41 occurred during the 2011 Tohoku-oki earthquake (Mw 9.0). This result shows that by
42 approximating tapered wedge geometry using a simple topographic parameter that can
43 be obtained from existing global bathymetry, we can quickly estimate the distribution of
44 frictional properties on a plate boundary fault along a trench and related seismic
45 activity.

46

47 **Keywords**

48 Subduction zone, Japan Trench, Critical taper model, Frictional variation, Accretionary

49 wedge

50 **Main Text**

51 **1. Introduction**

52 The first-order mechanics of a subduction zone wedge, a representative
53 feature of a fold-and-thrust belt, can be clearly explained by the critical taper model
54 (e.g., Dahlen 1990). This geomechanical model, which is based on the Mohr-Coulomb
55 failure criterion, allows frictional properties on a plate boundary fault to be determined.
56 This model is a key method for understanding megathrust earthquake mechanisms,
57 because direct measurements of plate boundary fault strength are quite rare and require
58 drilling into the deep décollement to obtain samples (e.g., Chester et al. 2013; Ujiie et al.
59 2013). According to this model, the tapered wedge geometry (slope angle α and basal
60 dip angle β) is determined by the strengths of the wedge materials and the effective
61 friction on the megathrust fault (μ_b') (Fig. 1). Thus, the critical taper model allows the
62 geomechanical condition of a subduction wedge to be determined. This information can
63 be used to compare geomechanical conditions among different subduction zones (e.g.
64 Dahlen 1990) or to examine their spatial distribution within a single subduction zone
65 (e.g., Fagereng 2011; Koge et al. 2014) or temporal changes along a single profile (e.g.,

66 Wang et al. 2010; Wang and Hu 2006). Slope angle α can be calculated from the
67 bathymetry above the subduction wedge, which is typically observed by a multi-beam
68 echosounder onboard a ship. Generally, the bathymetry is obtained with a vertical error
69 on the order of several meters, so the accuracy with which α is determined is sufficient
70 for characterizing the wedge geometry. However, the subsurface geometry parameter
71 used in critical taper model calculations, namely, the basal dip angle β , requires further
72 consideration. In a depth-converted profile of seismic reflection data, the depth to the
73 plate boundary fault depends strongly on the velocity model used, and the accuracy of
74 the depth-conversion process affects the value obtained for the topographic parameter β .
75 Therefore, unless only highly accurate depth-converted profiles are used to calculate
76 this critical taper model parameter, comparisons within and among wedges are likely to
77 be unreliable. On a scale of several kilometers, pre-stack depth migration (PSDM) data
78 or, at larger scale, a cross section of the velocity structure combined with refraction data
79 can be used for accurate determination of β for the critical taper model. However,
80 highly accurate PSDM data or seismic reflection profiles are often not available because
81 they require more processing time and are more costly to process than a simple

82 depth-converted profile. As a result, the number of accurate cross sections available for
83 a critical taper analysis is often insufficient to reveal detailed along-strike variations of
84 frictional properties in subduction zones.

85 **2. Revisiting, validating, and improving critical taper theory**

86 We first review formulations of Coulomb wedge/critical taper theory. All of
87 the formulas are based on a non-cohesive wedge model, which assumes non-viscosity
88 (Dahlen 1984). According to the Mohr-Coulomb failure criterion, $\tau = \sigma \cdot \tan\phi + C$,
89 where τ is shear stress, σ is vertical stress, ϕ is the internal friction coefficient (also
90 expressed as μ , the coefficient of internal friction averaged over the wedge), and C is the
91 cohesion force. Because internal friction forces are proportional to vertical stress
92 whereas cohesion forces are independent of vertical stress, the cohesion term can be
93 neglected when considering huge geological structures with large σ . Thus, the
94 noncohesive critical taper model is valid in the entire wedge.

95 Next, we theoretically verify the effect of the basal dip angle β on the
96 calculation of effective friction μ_b' and show that the effect of β becomes small when the
97 pore fluid pressure in the subduction zone is high. Hence, we propose that basal friction

98 in subduction zones can be inferred from only the slope angle α determined from the
99 bathymetry.

100 **2.1 Revisiting critical taper theory: Overview of the critical taper model to obtain** 101 **the effective coefficient of basal friction**

102 Critical taper theory (Davis et al. 1983; Dahlen 1984; Lehner 1986) is a
103 geomechanical model based on the Mohr-Coulomb failure criterion according to which
104 the wedge geometry (α and β) is constrained by the balance between wedge strength and
105 effective friction μ_b' (e.g., Adam and Reuther 2000).

106 In critical taper theory, we obtain μ_b' and the pore fluid pressure ratio (λ) in a
107 wedge by drawing cross plots between λ and μ_b' , as explained below (e.g., Adam and
108 Reuther 2000; Wang and Hu 2006; Wang et al. 2010, 2019) (Fig. 2). In the critical taper
109 theory formulation, the modified slope angle α' under subaerial conditions is formulated
110 as

$$111 \quad \alpha' = \tan^{-1} \left[\left(\frac{1 - \rho_w / \rho}{1 - \lambda} \right) \tan \alpha \right],$$

112 where α is a parameter obtained from the bathymetry/seismic profile, ρ is wedge
113 sediment density, ρ_w is fluid density, and λ is the pore fluid pressure ratio. Then, the

114 uniform angle between the most compressive principal stress axis σ_1 and the upper
115 slope, ψ_0 (see Fig. 1), is calculated as,

$$\psi_0 = \frac{1}{2} \sin^{-1} \left(\frac{\sin \alpha'}{\sin \phi} \right) - \frac{1}{2} \alpha'$$

116 where ϕ is the angle of internal friction within the wedge. Because along-strike stresses
117 are not considered in the critical taper model, the following simple geometric relation is
118 applicable (Fig. 1):

$$\alpha + \beta = \psi_b - \psi_0$$

119 where ψ_b is the angle between σ_1 and the basal plane. Then, the effective coefficient
120 of basal friction (μ_b') is obtained from the Mohr-Coulomb failure criterion τ and the
121 stress balance of the basal condition as

$$\mu_b' = \frac{\tan 2\psi_b}{\csc \phi \sec 2\psi_b - 1}$$

122 To draw the limb of the cross plot between μ_b' and λ , we set λ to range
123 between 0 and 1 (Fig. 2). The left limb of the critical state curve represents
124 extensionally critical states, and the right limb represents compressively critical states.
125 Then, under the assumption that λ is constant, we can obtain μ_b' from the intersection of
126 λ and the critical state curve calculated earlier.

127 For example, if we assume the mean wedge parameters $\rho = 2700 \text{ k/m}^3$, $\rho_w =$
128 1000 kg/m^3 , internal friction angle $\varphi = 34^\circ$, and $\lambda = 0.88$ (Lallemand et al. 1994) (Fig. 2),
129 μ_b' can be determined from the intersection of $\lambda = 0.88$ with the critical state curve
130 (Wang et al. 2019). Because the prism wedge in subduction zones should be in a
131 constant compressively critical state just before failure, we focus on only the
132 intersection with the right limb (representing compressively critical states). Thus, in this
133 example, we obtain $\mu_b' = 0.06$. For more details than are provided in this simple review,
134 please see the cited studies.

135 **2.2 Validation and improvement: Effects of the geometric parameters on μ_b'**

136 In this study, we examined the sensitivity of the calculated μ_b' to the assumed
137 α and β values to investigate how their accuracy affects the estimation of μ_b' . We used
138 the mean subduction zone parameter values in the example described in section 2.1 and
139 changed the values of α and β to see how μ_b' varied. The states of the frontal wedge with
140 $\alpha = 5^\circ$ and $\beta = 1^\circ$ or $\beta = 5^\circ$ are shown in Fig. 3A; in Fig. 3B both α and β are varied
141 from 1° to 5° . We allowed β to range from 1° to 5° because that range includes the basal
142 dip angle of most subduction zones (Lallemand et al. 1994; Wang et al. 2006). Here,

143 since μ_b' cannot be determined when $\alpha = \beta = 0$, those results were removed.

144 As a result—and this might be a blind spot in previous research—we found
145 that β has little influence on the estimation of μ_b' when the pore fluid pressure is high.
146 The change in β (from 1° to 5°) dominantly accounts for the change in the width of the
147 critical state curve (i.e., the angle between its limbs) between the two states illustrated in
148 Fig. 3A. When λ is high, the intersection between λ and the right limb of the critical
149 state curve is near the curve peak. Therefore, the change in the width due to a change in
150 β has only a slight effect on μ_b' . In typical subduction zones, λ is high (~ 0.88)
151 (Lallemand et al. 1994), so the effect of β should be regarded as a small one. Moreover,
152 this finding is also favorable in terms of the accuracy of μ_b' obtained by applying the
153 critical taper theory, because the seismic profile depth used to calculate β depends on
154 the velocity model/structure of the seismic profile, which is often not obtained with high
155 accuracy for reasons of time and money. Moreover, the number of available profiles is
156 also important to obtain the distribution of frictional properties by applying critical taper
157 theory. Thus, because β must be obtained from depth-converted profiles with low
158 accuracy, the resulting error is large (Koge et al. 2014). In contrast, α can be determined

159 with negligible error. The seafloor depth, which is used to calculate α , is mostly based
160 on multibeam data and the sound velocity profile of seawater. These can be acquired
161 with high accuracy by conductivity/temperature/depth (CTD) measuring systems, or by
162 deploying expendable bathythermograph (XBT) or XCTD instruments, which generally
163 have a vertical error on the order of several meters. Therefore, from this perspective, α
164 can be obtained with negligible error. The more significant factor influencing the error
165 of α is whether the obtained cross-section is aligned with the direction of maximum
166 slope. However, if the deviation from the maximum slope direction is no more than 18° ,
167 the error in α will be less than 5% [see Additional file 1]. Therefore, α can reliably be
168 obtained with high accuracy.

169 Under high pore fluid pressure conditions such as those in the mean
170 subduction zone, the influence of β on the calculation of μ_b' should be small enough to
171 ignore. Thus, the α variation can be used to approximate the relative along-trench
172 variation of μ_b' , and data accuracy is improved. In this first step, we considered as an
173 example the mean conditions described in section 2.1 (Fig. 3B and Table 1).
174 The next step is to determine quantitatively under what conditions β can be ignored and

175 the α - μ_b' approximation can be used. We used linear multiple regression analysis, a
176 statistical method that can be used to predict the value of a variable (the response
177 variable) from the value of two or more other variables (explanatory variables), to
178 determine whether α or β affects the effective friction coefficient μ_b' . Here, we used α
179 and β as explanatory variables and μ_b' as the response variable. We conducted this
180 analysis with the stats-model API in Python (Seabold and Perktold 2010). The obtained
181 regression equation is characterized by the coefficients of α and β (A and B ,
182 respectively) and the coefficient of multiple determination R^2 . To evaluate the relative
183 influence of α and β on μ_b' , we also defined the parameter “weight of alpha” (WOA) =
184 $A/(A + B)$. For the mean subduction zone, we obtained $R^2 = 0.99$ and $\text{WOA} = 77.50\%$.
185 Thus, the goodness of fit of the regression equation, indicated by R^2 , was high, and the
186 contribution of α to μ_b' was also high at 77.50%.

187 Next, to determine whether β can be neglected in most subduction zones, we
188 considered potential ranges of λ and φ in nature ($\lambda = 0-1$, $\varphi = 20-39^\circ$), and then
189 calculated WOA and R^2 for all combinations of λ and φ in these ranges (Fig. 4, raw data
190 in Additional file 2). For example, using mean subduction wedge values of 21

191 representative trenches (Lallemand et al. 1994), $(\lambda, \varphi) = (0.88, 34^\circ)$, and WOA =
192 78.02%. Of course, in some exceptional subduction zones, such as at the Sunda and
193 Makran trenches, λ is small (Wang and Hu 2006), so the appropriateness of the
194 application of the $\alpha-\mu_b'$ approximation needs to be considered carefully. For more
195 example, at the toe of the Japan Trench, Kimura et al. (2012) and Wang et al. (2019)
196 assumed the following parameters: $(\lambda, \varphi) = (0.8, 21.8^\circ)$ and $(\lambda, \varphi) = (0.95, 36^\circ)$,
197 respectively. Given that under these conditions, WOA = 79.86% and 88.54%,
198 respectively (Fig. 4), in the toe of the Japan Trench, the frictional variation in the wedge
199 can be roughly regarded as determined by α alone. Therefore, if the WOA of the
200 targeted subduction zone is sufficiently high, frictional conditions along the plate
201 interface can be obtained by using α alone.

202 **3. Application example of the $\alpha-\mu_b'$ approximation to the Japan Trench**

203 Through our review and verification of the critical taper model, we found that
204 β can be ignored not only when λ is high but also when WOA is high, owing to either
205 high λ or low φ (Fig. 4). Thus, in our approximation, the spatial variation in the slope
206 angle α is an indicator of the variation in the effective basal friction μ_b' , and, we can use

207 only bathymetry data to obtain the distribution of the friction coefficient within a single
208 subduction zone. Here, we apply this approximation to the Japan Trench. The Japan
209 Trench is suitable for the application of this method because, as shown in section 2.2,
210 WOA is high in the toe portion of the wedge and the friction coefficient along the plate
211 interface can thus be estimated from only α , as well as because a rupture occurred near
212 the trench axis during the 2011 Tohoku-Oki earthquake (Mw 9.0). Therefore, by
213 comparing the distribution of α which should reflect that of μ_b' in Japan Trench, the
214 question of why such coseismic rupture occurred in specific area can be addressed.

215 To apply our approximation model to the Japan Trench, we used the 250-m
216 grid data of Kishimoto (2000), focusing on the shallow portion within a horizontal
217 distance of 25 km from the trench axis, and obtained the distribution of α , interpreted as
218 the relative friction distribution, on the shallow megathrust (Fig. 5, Table 2). As a result,
219 using bathymetric profiles and slope angles obtained by modifying GMT/MATLAB
220 code as described by Wessel and Luis (2017), we accurately obtained the along-strike
221 distribution of μ_b' on the shallow plate boundary fault at 71 points (instead of at only a
222 dozen points or less, as is typical in applications of critical taper theory).

223 The low- α segment (low- μ_b' segment), located at approximately 36°–39°N,
224 corresponds to the coseismic slip distribution of the 2011 Tohoku-Oki earthquake
225 (Chester et al. 2013). This result suggests large fault rupture in the low- α segment have
226 occurred, causing the slip to propagate to the shallow portion of the plate boundary fault,
227 because of the low friction there. And it lead to the huge tsunami (e.g. Ide et al., 2011).
228 In contrast, the south and north ends of the coseismic slip zone are relatively
229 high-friction areas. As a result, the slip could not propagate to these other segments
230 because the high friction acted as a barrier. Therefore, the low friction in the shallow
231 area can be considered to be the cause of the huge tsunami. In addition, the low- α
232 segment identified here approximately corresponds to the central segment along the
233 Japan Trench (~37°–39°N) inferred from the distribution of seismic activity detected by
234 the S-net ocean-bottom seismograph network (Nishikawa et al. 2019).

235 Low-friction conditions might prevail generally along the Japan Trench
236 margin, except in regions of high friction caused by the recent subduction of a seamount
237 (Mochizuki et al. 2008) or the presence of petit-spot volcanoes (Hirano et al. 2006).
238 Because μ_b' depends on both λ and ϕ , it is not possible to determine whether variation in

239 α (i.e., relative μ_b') is due to a change in physical properties or to a change in pore fluid
240 pressure. Although here we cannot separate the effect of physical properties from that of
241 pore fluid pressure on α , both effects are reflected in the strength of the megathrust.

242 **4. Conclusion**

243 We presented an approach to the application of the critical taper model that,
244 intriguingly, has the potential to advance our ability to characterize basal friction along
245 the shallow plate interface in subduction zones. First, we reviewed the critical taper
246 model formulas used for calculating the effective coefficient of basal friction μ_b' . We
247 found that in most subduction zones, the effect of β on basal friction can be regarded as
248 slight, especially when WOA is high, which occurs when λ is high or φ is low. The
249 spatial variation of α can be easily obtained with high accuracy from bathymetry data
250 obtained by multi-beam observation. Even in areas where observation is difficult, there
251 are ETOPO1 (Amante and Eakins 2009) or other global datasets obtained by the
252 satellites, most of which are free to access and also have a vertical error of only a few
253 tens of meters (Varga and Bašić 2015). Note that these global data set based on
254 satellite observations, so the vertical error order is a little larger. Therefore, by applying

255 this approximation, the frictional distribution in subduction zones can now easily be
256 evaluated.

257 The approximated critical taper model proposed in this study can improve the
258 resolution of the along-trench distribution of μ_b' determined on a shallow megathrust.
259 By applying our approach to the Japan Trench, we showed that the seafloor slope angle
260 (relative μ_b') is systematically smaller within the area of large coseismic shallow slip
261 during the 2011 Tohoku-Oki earthquake than it is in areas to the south and north, where
262 little coseismic slip has been imaged. In the future, a global study is needed to examine
263 the correlation between frictional conditions along the plate interface as revealed by the
264 seafloor topography and seismicity and improve our understanding of the connection
265 between earthquake physics and tectonics. Our critical taper results are given in
266 Additional file 3, attached. By referring to this file, the coefficient of effective friction
267 on the plate boundary fault can be determined if the geomechanical parameters λ , φ , α ,
268 and β of the subduction zone are known.

269

270 **Declarations:** *Not applicable*

271 **Consent for publication:** *Not applicable*

272 **Availability of data and materials**

273 All data are available in the main text or in the supplementary materials.

274 **Competing interests**

275 Authors declare no competing interests.

276 **Funding**

277 HK was supported by JSPS KAKENHI Grant Number JP17K05687. JA

278 and JP are supported by JSPS KAKENHI Grant Number JP18H03732.

279 AM is supported by JSPS KAKENHI (Grant-in-Aid for Scientific

280 Research on Innovative Areas) Grant Number JP17H05321. SY is

281 supported by JSPS KAKENHI Grant Number 21H01189.

282 **Authors' contributions**

283 H. Koge mainly contributed to conceptualization, data curation,

284 methodology, visualization, and writing of the original draft. J. Ashi and

285 J.-O. Park conducted fundamental research on the geological settings of

286 subduction zones and contributed to the discussion. A. Miyakawa and S.

287 Yabe contributed to the methodology and discussion. All authors helped
288 to write, review, and edit the paper.

289 **Acknowledgements and Endnotes**

290 A. Yamaguchi, G. Kimura, and A. Noda provided advice on
291 fundamental research about frontal prisms. We acknowledge
292 anonymous reviewers for their thoughtful reviews.

293

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364

365

366 **Figure legends**

367

368 **Figure 1. Schematic illustration of the critical taper model.** **A** Cross section of the
369 forearc wedge in the Japan Trench (modified from Kimura et al. 2012). α : slope angle,
370 β : basal dip angle β , μ_b' effective friction on the megathrust fault. The frontal wedge
371 area is between the blue broken lines. **B** Diagram showing the self-similar growth of a
372 bulldozer wedge (modified from Dahlen 1990).

373

374 **Figure 2. Cross plot between the pore fluid pressure ratio λ and basal friction μ_b'**
375 **in the wedge.** All extensionally critical states form the left limb of the critical state
376 curve, and all compressively critical states form the right limb. The stable region is
377 under the curve (white). The straight-line intersecting the critical state curve represents
378 constant λ .

379

380 **Figure 3. Considering the weight of β .** **A** The mechanically critical value of a frontal
381 wedge is controlled by the fluid pressure ratio within the prism (λ) and the effective
382 basal friction (μ_b'). The solid and broken lines represent the critical state curve for

383 different values of β . **B** Variation in μ_b' when α and β are varied from 1° to 5° , assuming
384 mean subduction wedge conditions.

385

386 **Figure 4. Heat map for weight of alpha (WOA).** The closer WOA is to 100%, the
387 more friction can be considered in terms of seafloor topography alone, because μ_b' can
388 be determined from α alone. Conditions in the Japan Trench according to Kimura et al.
389 (2012) and Wang et al. (2019) are shown by the two white squares.

390

391 **Figure 5. Comparison of the spatial variation of slope angle α in the Japan Trench**
392 **and the coseismic slip distribution.** **A** Compiled coseismic slip along the Japan Trench
393 (red contours). The epicenter of the Tohoku-Oki earthquake is shown by a yellow star,
394 and the red lines show the positions of bathymetric profiles used to obtain α . **B** The
395 distribution of α along the Japan Trench. The red area corresponds to the coseismic slip
396 area in the map in **A** (Chester et al. 2013). The orange bar indicates the peak of the α
397 distribution histogram.

398

399 **Tables**

400

401 **Table 1. Values of μ_b obtained by varying α and β from 1° to 5° .** The left table was
402 calculated by assuming mean subduction wedge conditions. The right table was
403 calculated using conditions in the outer wedge of the Japan Trench.

404

405 **Table 2 Slopes measured along bathymetric profiles on the landward side of the**
406 **Japan Trench.**

407

408 **Additional files**

409 Additional file 1: Supplemental text.pdf

410 Additional file 2: result_ols.csv; raw data for WOA plot (Fig. 4)

411 Additional file 3: result_ct.csv; raw results for critical taper parameters.

Figures

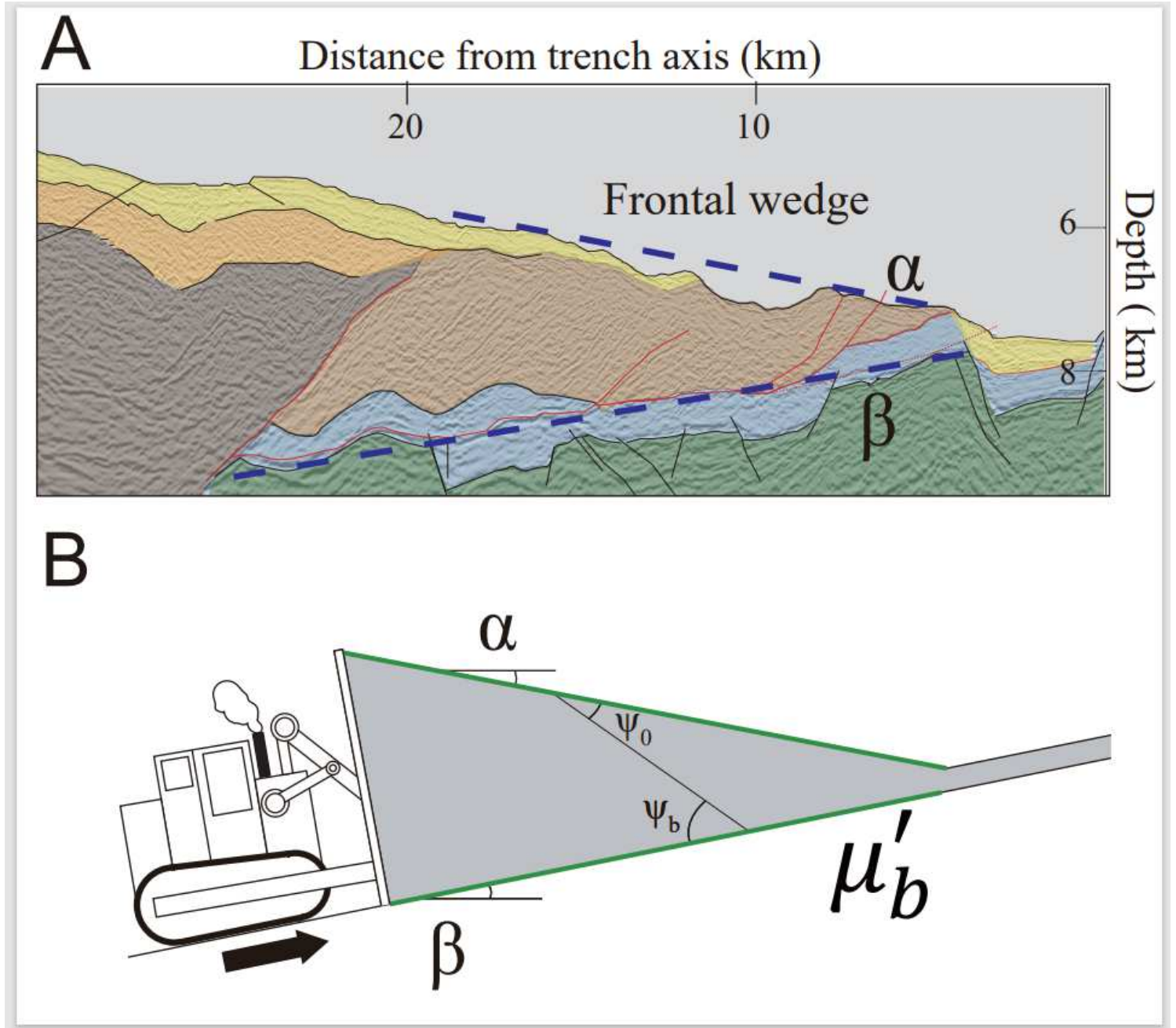


Figure 1

Schematic illustration of the critical taper model. A Cross section of the forearc wedge in the Japan Trench (modified from Kimura et al. 2012). α : slope angle, β : basal dip angle β , μ'_b effective friction on the megathrust fault. The frontal wedge area is between the blue broken lines. B Diagram showing the self-similar growth of a bulldozer wedge (modified from Dahlen 1990).

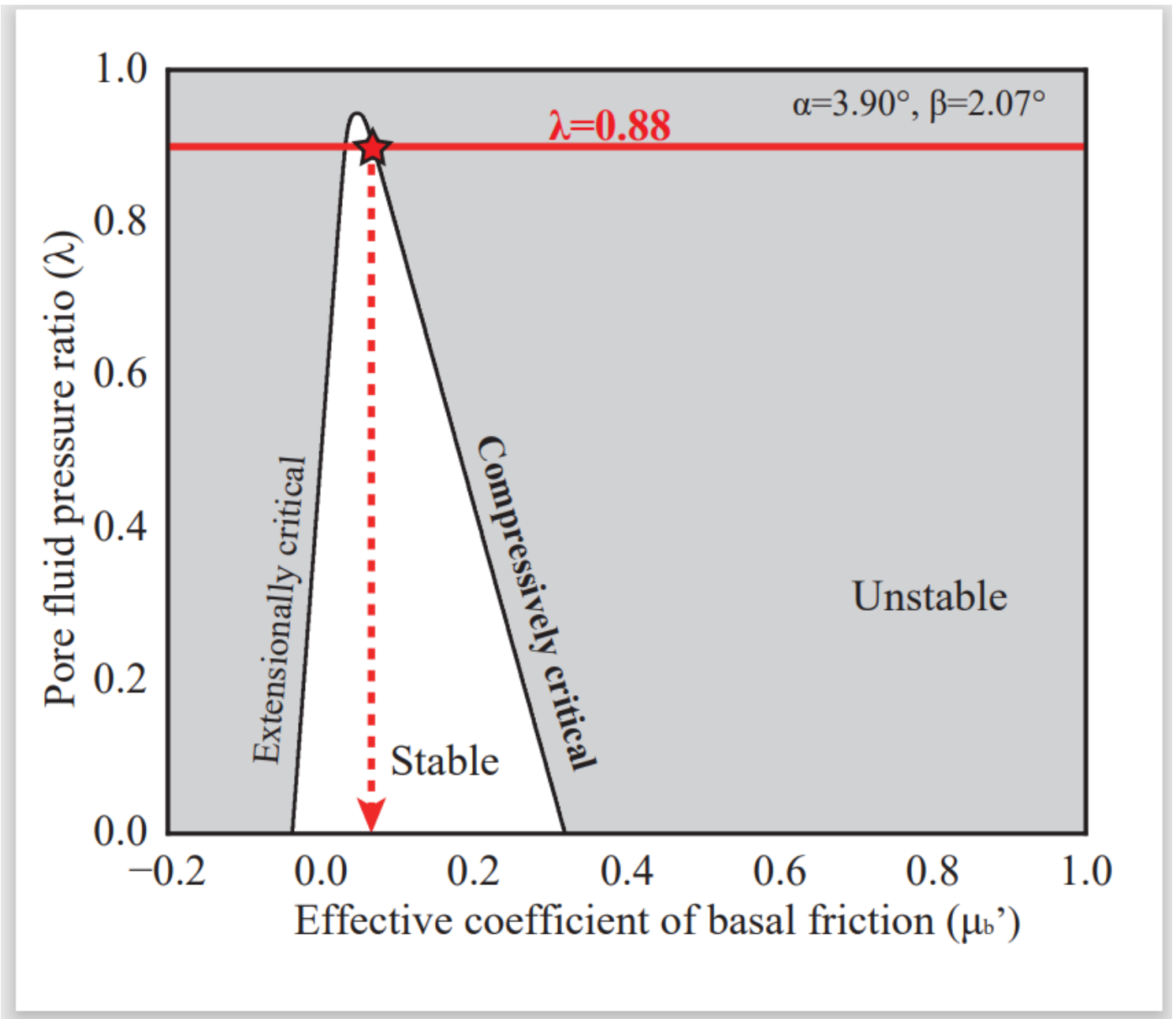


Figure 2

Cross plot between the pore fluid pressure ratio λ and basal friction μ_b' in the wedge. All extensionally critical states form the left limb of the critical state curve, and all compressively critical states form the right limb. The stable region is under the curve (white). The straight-line intersecting the critical state curve represents constant λ .

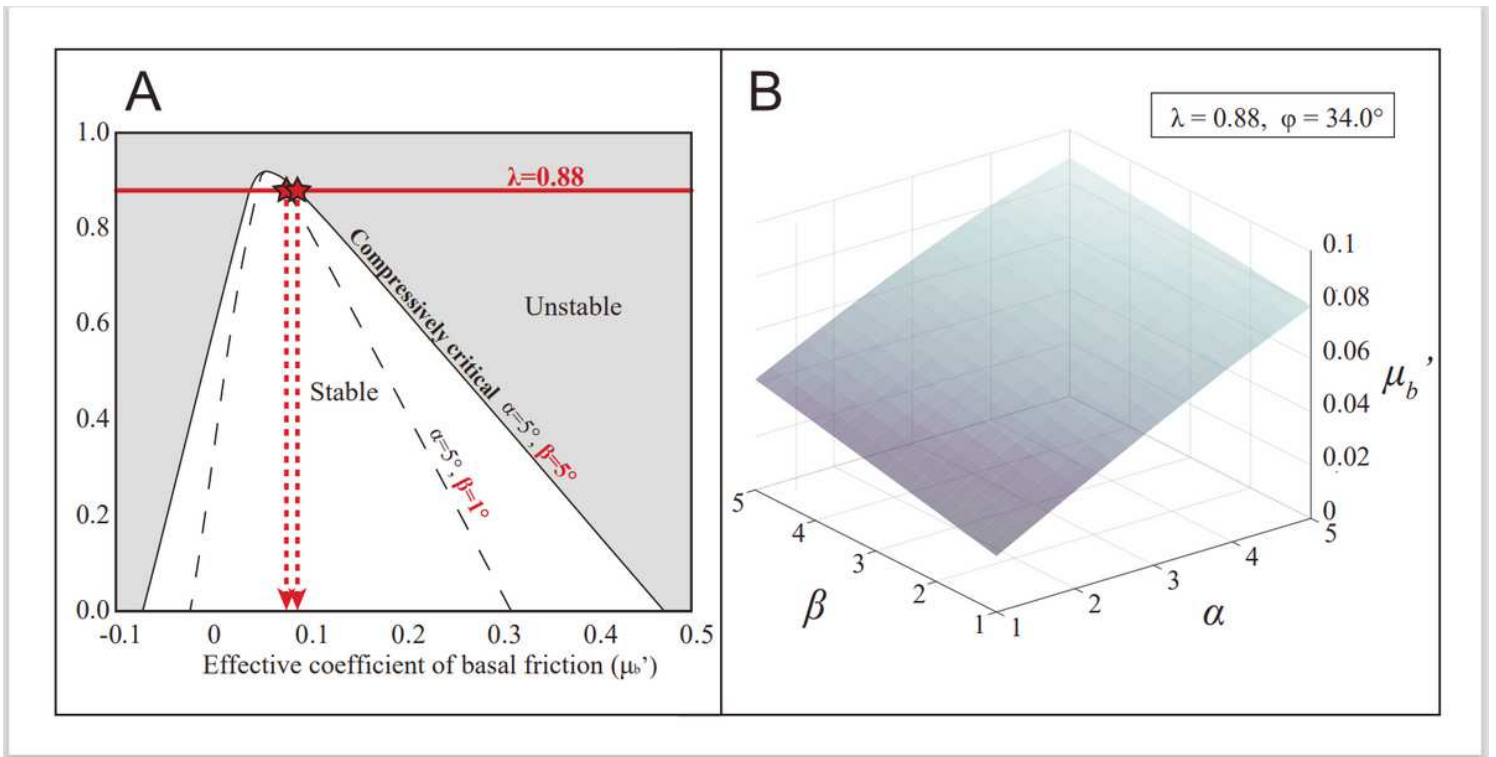


Figure 3

Considering the weight of β . A The mechanically critical value of a frontal wedge is controlled by the fluid pressure ratio within the prism (λ) and the effective basal friction (μ_b'). The solid and broken lines represent the critical state curve for different values of β . B Variation in μ_b' when α and β are varied from 1° to 5° , assuming mean subduction wedge conditions.

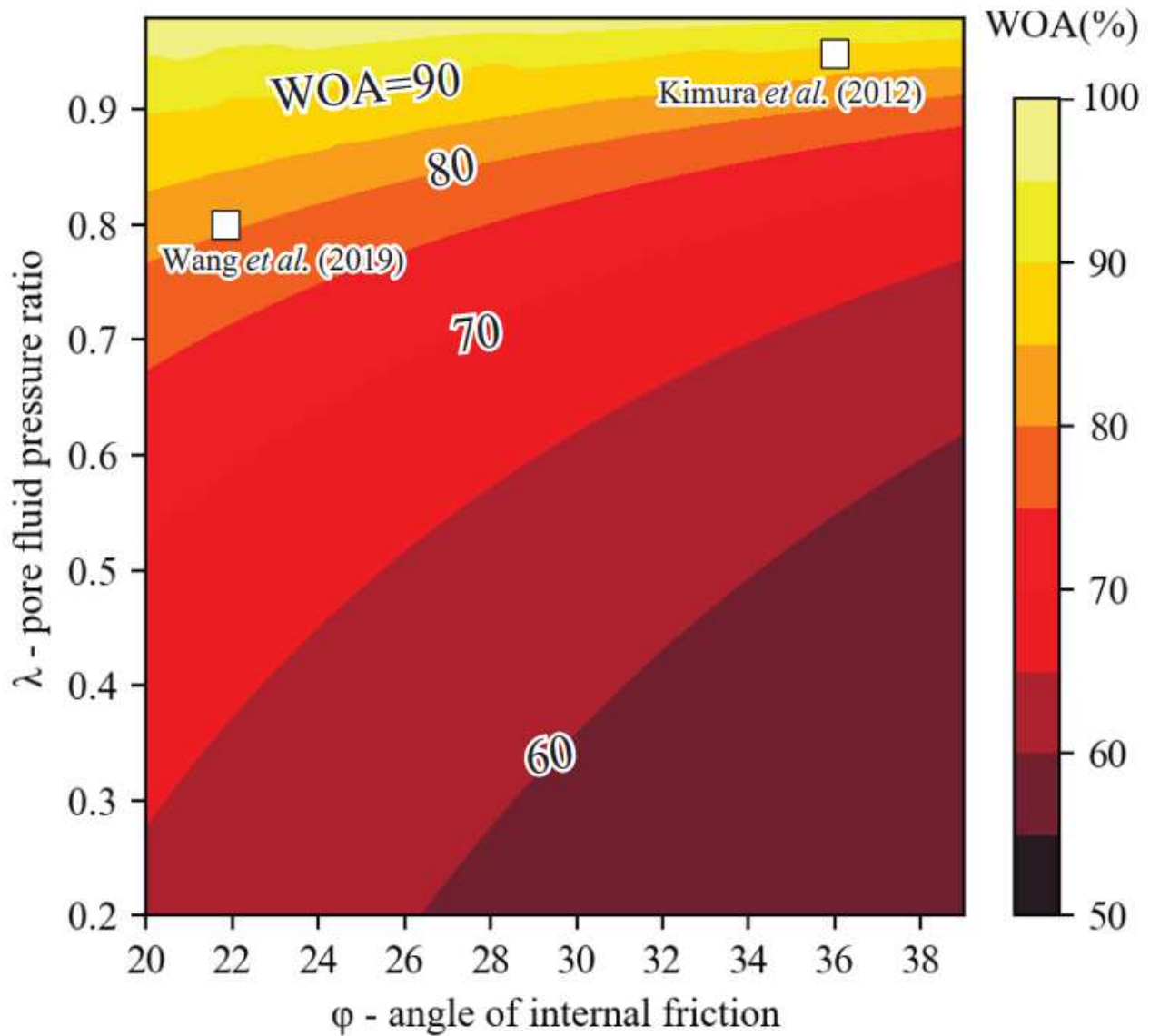


Figure 4

Heat map for weight of alpha (WOA). The closer WOA is to 100%, the more friction can be considered in terms of seafloor topography alone, because $\mu b'$ can be determined from α alone. Conditions in the Japan Trench according to Kimura et al. (2012) and Wang et al. (2019) are shown by the two white squares.

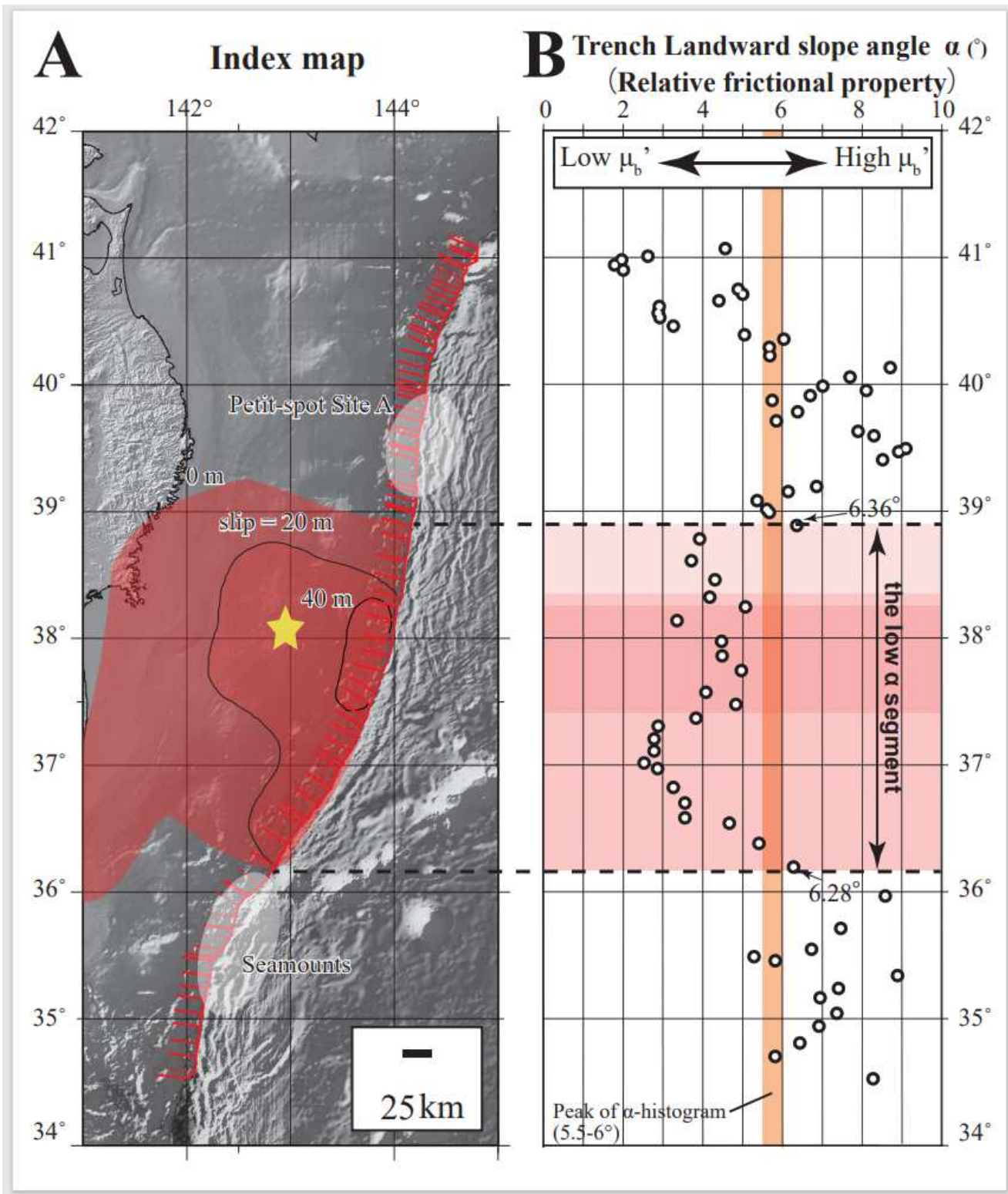


Figure 5

Comparison of the spatial variation of slope angle α in the Japan Trench and the coseismic slip distribution. A Compiled coseismic slip along the Japan Trench (red contours). The epicenter of the Tohoku-Oki earthquake is shown by a yellow star, and the red lines show the positions of bathymetric profiles used to obtain α . B The distribution of α along the Japan Trench. The red area corresponds to the

coseismic slip area in the map in A (Chester et al. 2013). The orange bar indicates the peak of the α distribution histogram.

Supplementary Files

This is a list of supplementary files associated with this preprint. Click to download.

- [FigureABSTRACT.jpg](#)
- [Supplementarytext.pdf](#)
- [resultols.csv](#)
- [resultct.csv](#)