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Altermagnetism: spin-momentum locked phase protected by non-relativistic symmetries

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Abstract

The search for novel magnetic quantum phases, phenomena and functional materials has been guided by relativistic magnetic-symmetry groups in coupled spin and real space¹⁻⁶ from the dawn of the field in 1950s¹⁻³ to the modern era of topological matter⁷⁻⁹. However, the magnetic groups cannot disentangle^{10,11} non-relativistic phases and effects, such as the recently reported unconventional spin physics in collinear antiferromagnets¹²⁻²⁹, from the typically weak relativistic spin-orbit coupling phenomena. Here we discover that more general spin symmetries in decoupled spin and crystal space^{10,30,31} categorize non-relativistic collinear magnetism in three phases: conventional ferromagnets and antiferromagnets, and a third distinct phase combining zero net magnetization with an alternating spin-momentum locking in energy bands, which we dub "altermagnetic". For this third basic magnetic phase, which is omitted by the relativistic magnetic groups, we develop a spin-group theory describing six characteristic types of the altermagnetic spin-momentum locking. We demonstrate an extraordinary spin-splitting mechanism in altermagnetic bands originating from a local electric crystal field, which contrasts with the conventional magnetic or relativistic splitting by global magnetization or inversion asymmetry. Based on first-principles calculations, we identify altermagnetic candidates ranging from insulators and metals to a parent crystal of cuprate superconductor. Our results underpin emerging research of quantum phases and spintronics in high-temperature magnets with light elements, vanishing net magnetization, and strong spin-coherence.

Main

The conventional symmetry theory of magnetic crystals considers transformations in coupled real physical space and the space of magnetic moment vectors. In other words, the rotation transformations acting on the coordinates of the atoms, subject to the standard crystallographic restrictions, simultaneously act on the components of the magnetic moment vectors^{4,30,31}. This symmetry formalism naturally arises from the classical orbital-current model of magnetic moments¹, as well as from the relativistic quantum-mechanical description of coupled spin and orbital degrees of freedom of electrons^{1,32}. The corresponding magnetic groups⁴ have been broadly applied in the research of equilibrium and non-equilibrium phenomena, including their modern topological variants^{7–9}, and have represented the primary tool for a systematic classification of hundreds of magnetic structures in materials’ databases^{5,6}.

A spin-group formalism is a vast generalization of the conventional magnetic groups^{10,30,31}. It considers pairs of transformations $[R_1 \parallel R_2]$, where the transformations on the left of the double vertical bar act only on the spin space and on the right of the double vertical bar only on the real space^{10,30,31}. The symmetry landscape of the spin groups is much richer because, in general, different rotation transformations can simultaneously act on the spin and real space, and only the transformations in the real space are crystallographically-restricted. Despite their richness, studies based on the spin symmetries have appeared only sporadically in literature. For example, they were applied for the classification of possible spin arrangements on crystals, with an emphasis on complex non-collinear or disordered structures¹¹. Overall, however, the spin-group formalism has remained unexploited.

The key significance of the spin groups is that they can offer a systematic symmetry description of physics arising from non-relativistic electro-magnetic crystal potentials, which typically play the leading role in magnetism^{10,11}. Here by the electric crystal potential we refer to the internal potential in the non-magnetic phase of the crystal, as described, e.g., by the local-density approximation of the density functional theory (DFT); by the additional magnetic component we refer to the modification of the internal crystal potential due to the transition to the magnetically ordered phase. Since the magnetic groups represent only a small subset of the spin groups³¹, they are prone to omit prominent magnetic phases dominated by the non-relativistic electro-magnetic crystal potentials. For example, the

magnetic groups can only determine whether a net magnetization is allowed or not, but do not distinguish ferromagnets from antiferromagnets in which magnetization arises only as a weak relativistic perturbation¹. For the band structures, the magnetic groups were only used to identify a violation of Kramers spin-degeneracy, again without disentangling the non-relativistic and relativistic origin^{33,34}.

The central topic of our work is the altermagnetic phase of collinear magnets, which we delimit using the non-relativistic spin groups from a ferromagnetic phase with non-zero net magnetization, and from a Kramers spin-degenerate antiferromagnetic phase. Altermagnets have split, but equally populated spin-up and spin-down energy iso-surfaces. The corresponding planar or bulk spin-momentum locking is protected by the spin-group symmetries, and can be characterized by an even-integer spin winding number.

We discover an extraordinary microscopic spin-splitting mechanism in altermagnetic materials which originates from a local anisotropic electric crystal field, i.e., from crystal properties of the non-magnetic phase. It is fundamentally distinct from the earlier considered internal magnetic-interaction mechanisms^{14,17,19,28,35}, such as the anisotropic spin-dependent hopping in the magnetic state^{19,28}. The altermagnetic spin-splitting by the local electric crystal field also starkly contrasts with the conventional mechanisms of the ferromagnetic splitting due to the global magnetization, or the spin-orbit splitting due to the global inversion asymmetry. It opens a third paradigm for designing spin quantum phases of matter based on the strong crystal-field effects, complementing the widely explored relativistic or many-body phenomena³⁶.

The spin-groups describing the altermagnetic phase have no correspondence in the magnetic groups. The recent reports^{12–29} pointing towards uncharted Berry phase or charge-spin conversion physics then not only highlight the range of potential science and technology implications of this new magnetic phase, but also the importance of its proper symmetry description by the non-relativistic spin groups.

Derivation of spin group categorization of non-relativistic collinear magnetism

We start with the derivation of three distinct spin group types by which we categorize all non-relativistic collinear magnets into the ferromagnetic, Kramers spin-degenerate antiferromagnetic, and altermagnetic phases. In general, spin groups can be expressed as a direct

product of so-called spin-only groups, containing transformations of the spin space alone, and so-called non-trivial spin groups containing the elements $[R_1 \parallel R_2]$, but no elements of the spin-only group^{30,31}. For the collinear spin arrangements on crystals, the spin-only group is given by^{30,31} $\mathbf{C}_\infty + \bar{C}_2\mathbf{C}_\infty$. Here $\mathbf{C}_\infty$ is a group representing all rotations of the spin space around the common axis of spins, and $\bar{C}_2$ is a 180° rotation around an axis perpendicular to the spins, combined with the spin-space inversion. We emphasize that because of the absence of the spin-only group symmetries in magnetic groups, the collinear spin groups have no correspondence in the magnetic groups. In other words, unlike the spin groups, the conventional relativistic magnetic groups do not strictly delimit collinear magnets.

Next we point out that the spin-space inversion in the spin groups enters via the time-inversion^{11,30,31}. Since time is common in both spin and real space, the spin-space inversion is accompanied by a simultaneous time-inversion in the real space ($\mathcal{T}$). Although $\mathcal{T}$ acts as identity on the real space coordinates of the atoms, it flips the sign of the crystal momentum. This is important for the band-structure spin symmetries. In particular, we will now use the symmetry $[\bar{C}_2 \parallel \mathcal{T}]$, which follows directly from the above spin-only group of the collinear magnets, and from the simultaneous action of the time-inversion on the spin and real (momentum) space. When applying the transformation $[\bar{C}_2 \parallel \mathcal{T}]$ on spin (s) and crystal-momentum ($\mathbf{k}$) dependent bands $\epsilon(s, \mathbf{k})$, we obtain $[\bar{C}_2 \parallel \mathcal{T}]\epsilon(s, \mathbf{k}) = \epsilon(s, -\mathbf{k})$. Next, since $[\bar{C}_2 \parallel \mathcal{T}]$ is a symmetry of non-relativistic collinear spin arrangements on crystals, $[\bar{C}_2 \parallel \mathcal{T}]\epsilon(s, \mathbf{k}) = \epsilon(s, \mathbf{k})$, and hence $\epsilon(s, \mathbf{k}) = \epsilon(s, -\mathbf{k})$. The bands are invariant under real-space (crystal-momentum) inversion even if the crystal lacks the real-space inversion symmetry.

We now move on to the non-trivial spin groups which are obtained by combining the groups of real-space crystallographic transformations with the groups of spin-space transformations^{30,31}. Regarding the real-space crystallographic groups, we can limit our basic classification to the Laue groups, which are the crystallographic point groups containing the real-space inversion symmetry element. The corresponding spin Laue groups describe the non-relativistic spin-momentum locking, which is present in the band structure independent of the crystal's real-space translation symmetries, and independent of whether the crystal does or does not have the real-space inversion symmetry. The independence of translations is straight forward, and the invariance of bands under real-space (crystal-momentum) inversion was derived above from the spin-only group symmetry of the collinear

spin arrangements. (Note that additional symmetry analysis of complex band structures, based on the direct extension of the theory to spin space groups, is beyond the scope of the present work.)

Regarding the groups of spin-space transformations, there can be some freedom in their choice^{30,31}. For the collinear spin arrangements, one of the two spin-space transformation groups is $\mathbf{S}_1 = \{E\}$, i.e., contains just the spin-space identity³⁰. We choose the second group in the form of $\mathbf{S}_2 = \{E, C_2\}$ which is favorable for our derivation of the categorization into the three phases of non-relativistic collinear magnets. The group contains the spin-space identity and the 180° rotation of the spin space around an axis perpendicular to the spins. (We note that because of the above spin-only group symmetry element $\bar{C}_2$, and because the product of spin-space transformations $\bar{C}_2 C_2$ is equal to the spin-space inversion, an alternative choice³⁰ of $\mathbf{S}_2$ contains the spin-space inversion instead of C_2 .)

We construct all the non-trivial spin (Laue) groups, whose elements on the left of the double vertical bar form a group of the spin-space transformations and on the right of the double vertical bar a (Laue) group of the real-space crystallographic transformations, by using the isomorphism theorem³⁰. It implies the procedure of combining all isomorphic coset decompositions of the two groups, i.e., decompositions with the same number of cosets for the two groups³⁰. (A coset decomposition of a group $\mathbf{X}$ is given by $\mathbf{X} = \mathbf{x} + X_1\mathbf{x} + X_2\mathbf{x} + \dots$, where $\mathbf{x}$ is a subgroup of $\mathbf{X}$ and X_i are elements of $\mathbf{X}$ ³⁰.) The details of our derivation are in Supplementary Sec. I. Here we summarize the result in which all the non-trivial spin Laue groups describing $\epsilon(s, \mathbf{k})$ of collinear magnets are arranged into the following three distinct types using the isomorphic coset decompositions.

The first type of the non-trivial spin Laue groups is given by $\mathbf{R}_s^{\text{I}} = [E \parallel \mathbf{G}]$, where $\mathbf{G}$ is the crystallographic Laue group. Because there are 11 different crystallographic Laue groups, there are also 11 different $\mathbf{R}_s^{\text{I}}$ groups. As highlighted in Fig. 1, the $\mathbf{R}_s^{\text{I}}$ groups do not imply spin degeneracy of $\epsilon(s, \mathbf{k})$ at any $\mathbf{k}$ -point. They describe non-relativistic band structures of collinear ferromagnets.

The second type of the non-trivial spin Laue groups is given by $\mathbf{R}_s^{\text{II}} = [E \parallel \mathbf{G}] + [C_2 \parallel \mathbf{G}]$. Here the $[C_2 \parallel E]$ symmetry (recall that $\mathbf{G}$ is a group containing the real-space identity E element) implies spin-degeneracy of $\epsilon(s, \mathbf{k})$ for all $\mathbf{k}$ -vectors in the Brillouin zone. The 11 different $\mathbf{R}_s^{\text{II}}$ groups describe non-relativistic band structures of non-magnetic crystals, as well as Kramers spin-degenerate bands of collinear antiferromagnets (see Fig. 1). The corre-

sponding antiferromagnetic spin arrangements on crystals have a symmetry $[C_2 \parallel \mathbf{t}]$, which interchanges atoms and rotate the spin by 180° between opposite-spin sublattices. Here $\mathbf{t}$ on the right side of the double vertical bar is a real-space translation. Examples^{37,38} are antiferromagnets FeRh or MnBi₂Te₄. The $\mathbf{R}_s^{\text{II}}$ groups also describe Kramers spin-degenerate collinear antiferromagnetism in crystals with the opposite-spin-sublattice transformation symmetry $[C_2 \parallel \bar{E}]$, where $\bar{E}$ on the right side of the double vertical bar is the real-space inversion (see Supplementary Sec. I). Here examples^{39,40} are antiferromagnets CuMnAs or Mn₂Au.

The remaining third distinct type of the non-trivial spin Laue groups is given by

$$\mathbf{R}_s^{\text{III}} = [E \parallel \mathbf{H}] + [C_2 \parallel A] [E \parallel \mathbf{H}] = [E \parallel \mathbf{H}] + [C_2 \parallel \mathbf{G} - \mathbf{H}], \quad (1)$$

with A representing a real-space proper or improper rotation which interchanges atoms between opposite-spin sublattices. We see from Eq. (1) that for $\mathbf{R}_s^{\text{III}}$, $\mathbf{G}$ is expressed as a sublattice coset decomposition, where $\mathbf{H}$ contains only the real-space transformations which interchange atoms between same-spin sublattices, and $\mathbf{G} - \mathbf{H}$ contains only the real-space transformations which interchange atoms between opposite-spin sublattices. Lifted spin-degeneracies in the $\mathbf{R}_s^{\text{III}}$ groups are allowed for crystal momenta whose little group does not contain $\mathbf{H}A$ elements. They satisfy $\mathbf{H}A\mathbf{k} = \mathbf{k}' \neq \mathbf{k}$, implying that $\epsilon(s, \mathbf{k}) = [C_2 \parallel \mathbf{H}A]\epsilon(s, \mathbf{k}) = \epsilon(-s, \mathbf{k}')$ (see Fig. 1). It guarantees that the spin-up and spin-down energy iso-surfaces are split, but have the same number of states. These non-relativistic band structure signatures of the $\mathbf{R}_s^{\text{III}}$ altermagnetic phase are unparalleled in the $\mathbf{R}_s^{\text{I}}$ ferromagnetic or $\mathbf{R}_s^{\text{II}}$ Kramers-degenerate antiferromagnetic phases. Simultaneously, there are 10 different $\mathbf{R}_s^{\text{III}}$ groups which is comparable to the number of the $\mathbf{R}_s^{\text{I}}$ or $\mathbf{R}_s^{\text{II}}$ groups, suggesting that altermagnetism is abundant. The 10 non-trivial spin Laue groups of altermagnets are listed in Tab. 1, where we adopted Litvin's notation of the spin groups³¹. Note, that they are constructed from only 8 different crystallographic Laue groups. On the hand, the altermagnetic spin Laue groups cannot be constructed for the 3 remaining crystallographic Laue groups, namely from $\mathbf{G} = \bar{1}, \bar{3}$ or $m\bar{3}$.

Before moving to the analysis of the altermagnetic spin-momentum locking protected by the symmetries of the spin-group, we emphasize additional differences from the magnetic groups. The latter are constructed by combining crystallographic groups (with the same transformations acting simultaneously on coordinates of atoms and components of mag-

netic moment vectors) with one group containing the identity element alone, and a second group containing the identity and the time-inversion. Comparing this to the spin-group formalism with $\mathbf{S}_1$ also containing only the identity element and $\mathbf{S}_2$ with again two elements implies, that for describing all magnetic structures, the relativistic symmetry formalism has the same number of different magnetic groups as is the number of different spin groups describing exclusively collinear spin arrangements. Also, because of the crystallographic operations applied in the coupled real and spin space, there is no counterpart in magnetic groups of the sublattice coset decomposition form of the altermagnetic $\mathbf{R}_s^{\text{III}}$ spin groups (see Supplementary Sec. I). As we further highlight below, the decomposition into same-spin and opposite-spin-sublattice transformations in $\mathbf{R}_s^{\text{III}}$ plays a central role in the understanding of altermagnetism.

Altermagnetic spin-momentum locking protected by spin symmetries

We now discuss basic characteristics of the spin-momentum locking in altermagnets. The Γ -point is invariant under all real-space transformations. The $[C_2 \parallel A]$ symmetry present in the $\mathbf{R}_s^{\text{III}}$ groups thus guarantees spin-degeneracy of the Γ -point. On the other hand, lifted spin-degeneracies in the rest of the Brillouin zone, including other time-reversal invariant momenta, are not generally excluded in altermagnets. We have already derived above that the bands are symmetric with respect to the inversion of $\mathbf{k}$. Moreover, the collinearity, protected by the spin-only group symmetries, implies that spin is a good quantum number and spins have a common $\mathbf{k}$ -independent quantization axis across the non-relativistic band structure. These basic spin-momentum locking characteristics of altermagnets are in striking contrast to the relativistic band structures of non-magnetic crystals. The latter systems have all time-reversal invariant momenta spin-degenerate, and the spin-momentum locking due to the broken real-space inversion symmetry is odd in $\mathbf{k}$, and has a form of a continuously varying spin-texture in the momentum space⁴¹.

Other prominent spin-momentum locking features in altermagnets are protected by the specific $[C_2 \parallel A][E \parallel \mathbf{H}]$ symmetries present in the given $\mathbf{R}_s^{\text{III}}$ group. For example, a symmetry $[C_2 \parallel M_c]$, where c is the axis perpendicular to the $a - b$ mirror plane, defines a spin-degenerate $k_a - k_b$ nodal plane at $k_c = 0$, or other k_c separated from $M_c k_c = -k_c$ by a reciprocal lattice vector. This is because $[C_2 \parallel M_c]$ transforms a wavevector from this plane

on itself, or on an equivalent crystal momentum separated by the reciprocal lattice vector, while spin is reversed. Similarly, a $[C_2 \parallel C_{n,c}]$ symmetry, where $C_{n,c}$ is an n -fold rotation symmetry around the c -axis, imposes a spin-degenerate nodal-line parallel to the k_c -axis for wavevectors with $k_a = k_b = 0$, or other $k_{a(b)}$ separated from $C_{n,c}k_{a(b)}$ by a reciprocal lattice vector. We note that the high symmetry planes or lines are typically of main focus when assessing the electronic structures. This may explain why, apart from the omission by the conventional magnetic groups, altermagnets remained unnoticed during the decades of DFT and experimental studies of band structures.

Each of the 10 spin Laue groups of altermagnets can be assigned a characteristic spin winding number. In Tab. 1 we show the spin-momentum locking with the corresponding spin winding number depicted on top of model $\mathbf{k} \cdot \mathbf{p}$ Hamiltonian bands (see Supplementary Sec. II). We obtain either planar (cf. relativistic Rashba or Dresselhaus spin-texture) or bulk (cf. relativistic Weyl spin-texture) non-relativistic spin-momentum locking, with the characteristic spin winding number $W = 2, 4$, or 6 , when integrated over a surface near and enclosing the Γ -point. (Further from the Γ -point, additional band-crossings can result in higher even-integer winding numbers.) The planar altermagnetic spin-momentum locking is relevant for (quasi)two-dimensional and three-dimensional crystals, while the bulk spin-momentum locking only for three-dimensional crystals. We note that the earlier reported materials^{13–29,34,42,43} FeF_2 , MnO_2 , RuO_2 , $\kappa\text{-Cl}$, MnF_2 , Mn_5Si_3 , LaMnO_3 , FeSb_2 , CaCrO_3 , referred to as unconventional spin-split antiferromagnets in these studies, all correspond to the altermagnetic class with the characteristic planar spin winding number $W = 2$.

A complementary orbital-harmonic representation¹⁹ allows us to identify a d -wave, g -wave, or i -wave form of the anisotropic spin-momentum locking near the Γ -point. The list of characteristic (not exclusive) anisotropic crystal harmonics, given in Supplementary Sec. II, facilitated the derivation of the model $\mathbf{k} \cdot \mathbf{p}$ Hamiltonian bands of altermagnets shown in Tab. 1.

Spin-splitting by local electric crystal field

We now demonstrate the spin-momentum locking protected by spin-group symmetries, and the microscopic spin-splitting mechanism due to the local electric crystal field, on an altermagnetic spin arrangement on the crystal of KRu_4O_8 . The real-space crystal structure

of KRu_4O_8 , as reported in earlier studies^{44,45}, is schematically illustrated in Fig. 2a. The symmetry of the lattice is body-centred tetragonal (crystallographic space group $I4/m$). Purple and cyan color in Fig. 2a represent the collinear antiparallel spin arrangement on the crystal. In addition, the A and B symbols label the real-space sublattices corresponding to the opposite spins in the altermagnetic phase. The A and B real-space sublattices are strongly anisotropic, and related by a mutual planar rotation by 90° (C_{4z}). Correspondingly, the non-trivial spin Laue group describing the spin-momentum locking in the altermagnetic phase is $2_4/1_m$. According to Eq. (1), it can be decomposed as,

$$2_4/1_m = [E \parallel 2/m] + [C_2 \parallel C_{4z}] [E \parallel 2/m]. \quad (2)$$

Fig. 2b shows the DFT calculation of the spin-momentum locking, protected by the spin-group symmetries, on top of two selected KRu_4O_8 Fermi surface sheets. (The band structure was obtained using the DFT full-potential linearized augmented plane-wave code ELK within the local-spin-density approximation⁴⁶.) In particular, the $[C_2 \parallel C_{4z}]$ symmetry leads to three spin-degenerate nodal lines parallel to the k_z -axis, $[0, 0, k_z]$, $[2, 0, k_z]$, and $[0, 2, k_z]$, marked by grey points in Fig. 2b (here the wavevectors are in units of π divided by the lattice constant). The latter two correspond, for $k_z = 0$, to time-reversal invariant momenta $\mathbf{M}_1$ and $\mathbf{M}_2$. On the other hand, the spin-degeneracy is strongly lifted at time-reversal invariant momenta $\mathbf{X}$ and $\mathbf{Y}$, corresponding to the directions of the real-space anisotropy axes of the two sublattices. Consistently, the little crystallographic Laue group at the $\mathbf{X}$ and $\mathbf{Y}$ wavevectors is $2/m$, which coincides with the halving subgroup of same-spin-sublattice transformations. The resulting spin winding number is $W = 2$. The spin-momentum locking is planar, reflecting the real-space planar mutual rotations of the crystal-anisotropies of the opposite-spin sublattices.

We now move on to the demonstration of the electric crystal-field mechanism of the spin-splitting, which we compare to the more conventional magnetic mechanism. The analysis is presented in Figs. 2c-g. Energy bands in the non-magnetic and altermagnetic phase are shown in Figs. 2c,d. The high-energy band around 0.9 eV in the depicted portion of the Brillouin zone is two-fold spin-degenerate in the non-magnetic phase (upper part of Fig. 2c). The magnetic component of the internal electro-magnetic crystal potential in the altermagnetic phase generates an anisotropic $\mathbf{k}$ -dependent spin splitting, as shown in the upper part of Fig. 2d where the purple and cyan color correspond to opposite spin states. The

sign of the spin splitting alternates, following the symmetries of the spin group. This type of the spin-splitting belongs to a family, generally referred to as internal magnetic-interaction mechanisms^{14,17,19,28}. Note that another example, considered earlier in the literature, is a Pomeranchuk Fermi liquid instability in an anisotropic (d -wave) spin-triplet channel¹⁴. In contrast to this correlated physics interpretation, we identify the spin splitting without including correlation effects beyond the local-spin-density approximation.

The other bands of KRu_4O_8 , for energies near the Fermi level, also show a spin splitting within the DFT band-structure theory. However, here the microscopic origin is in the electric crystal field, i.e., it is fundamentally distinct from the internal magnetic-interaction mechanisms. In the non-magnetic phase, we observe in the lower part of Fig. 2c a couple of two-fold spin-degenerate bands whose mutual splitting (highlighted by grey shading) by the electric crystal field is $\mathbf{k}$ -dependent, merging at the four-fold degenerate Γ , $\mathbf{M}_1$ and $\mathbf{M}_2$ points. Remarkably, the $\mathbf{k}$ -dependent spin-splitting in the antiferromagnetic phase in the lower part of Fig. 2d (highlighted again by grey shading) copies the $\mathbf{k}$ -dependent band splitting by the electric crystal field in the non-magnetic phase. Its microscopic explanation is provided in Figs. 2f,g.

We start the discussion of Fig. 2f from the projections of the bands on the sublattice A and B in the non-magnetic phase (black lines). The projections are dominated by Ru d_{xz} and d_{yz} orbitals. This is in agreement with earlier report⁴⁵, which showed the presence of Ru t_{2g} orbitals near the Fermi level. At the Γ -point, the A and B projected bands are degenerate, which is consistent with the octahedral environment with the tetragonal symmetry⁴⁷. Including spin, the Γ -point is then four-fold degenerate in the non-magnetic phase.

The band whose dominant weight is on sublattice A is strongly anisotropic with respect to $\mathbf{k}$ when moving towards the $\mathbf{X}$ and $\mathbf{Y}$ points (left panel of Fig. 2f). The same applies to the sublattice B band, however, the sense of the anisotropy reverses (right panel of Fig. 2f). The band anisotropies reflect the strong local crystalline anisotropy, conspiring with the favorable symmetry of the involved orbitals. The local crystalline anisotropy is described by the elements of the halving subgroup $2/m$, which interchange atoms within the same sublattice. On the other hand, the reversed sense of the anisotropies of the sublattice A and B bands reflects the real-space rotation symmetry C_{4z} , which interchanges atoms between sublattice A and B. By adding up the A and B projections we obtain the bands shown in

Fig. 2c. They progressively split by the electric crystal field when the $\mathbf{k}$ -vector moves from the Γ -point towards, e.g., the $\mathbf{X}$ point, with the lower band dominated by one sublattice and the upper band by the other sublattice. Along the $\Gamma - \mathbf{Y}$ line, the sublattice indices of the lower and upper bands switch places.

The bands in the altermagnetic phase, projected again on the sublattice A and B, are also plotted in Fig. 2f. As in Fig. 2d, the purple and cyan color correspond to opposite spins. We see that for bands with dominant weight on sublattice A, spin states shown in purple move up in energy while the opposite spin states shown in cyan move down (left panel of Fig. 2f). The magnetic component of the internal crystal potential in the altermagnetic phase generates in this case a splitting (highlighted by light-blue shading) which is nearly $\mathbf{k}$ -independent. This scenario is fundamentally distinct from the strongly $\mathbf{k}$ -dependent magnetic splitting of the high-energy band, shown in Fig. 2e. It is reminiscent of ferromagnets. However, unlike the common ferromagnetic case, the nearly $\mathbf{k}$ -independent magnetic splitting reverses sign in our altermagnet for the sublattice B bands (right panel of Fig. 2f). This locality, in which band states near the Fermi level with one spin have a dominant weight on one sublattice, is again distinct from the delocalized nature of spin states in the high-energy bands shown in Fig. 2e. It also starkly contrasts with the conventional mechanisms of the ferromagnetic splitting of band spin-states experiencing the global magnetization, or the spin-orbit splitting due to the global electric inversion asymmetry. An additional illustration of the locality is shown in Fig. 2g where we plot the real-space DFT spin-density around the Ru atom in sublattice A and B. Consistent with the spin Laue group symmetry and the dominant d_{xz} and d_{yz} orbitals near the Fermi level, the opposite-spin local densities in the two sublattices are highly anisotropic, with the mutually rotated real-space anisotropy axes.

Adding up the A and B sublattice projections of Fig. 2f then explains the formation of two pairs of spin-split bands seen in Fig. 2d. The mutual magnetic splitting between the two pairs is nearly $\mathbf{k}$ -independent, while the spin splitting within each pair is a $\mathbf{k}$ -dependent copy of the band splitting by the local anisotropic electric crystal field in the non-magnetic phase (Fig. 2c). It also explains that the two pairs have opposite sign of the spin splitting and that, within each pair, the spin-splitting sign is opposite when moving from the Γ -point point towards the $\mathbf{X}$ or $\mathbf{Y}$ points. We see from Figs. 2d and 2f, that even if the nearly $\mathbf{k}$ -independent magnetic splitting were small, the local electric crystal field would still determine the splitting between the two nearest bands with opposite spin in the

altermagnetic phase at $\mathbf{k}$ -vectors sufficiently close to the Γ -point. This is a consequence of the nearly $\mathbf{k}$ -independent magnetic band-splitting, and of the spin-degeneracy of the Γ -point in altermagnets.

In the studied KRu_4O_8 altermagnet, the spin-splitting originating from this extraordinary electric crystal-field mechanism reaches a 300 meV scale. In Supplementary Sec. III and Fig. S1 we show that in altermagnetic RuO_2 , a spin splitting reaching a 1 eV scale^{13,14,28} is also due to the electric crystal-field mechanism. These altermagnetic spin-splitting magnitudes are comparable to spin splittings in ferromagnets but, unlike ferromagnets, are accompanied by a zero net magnetization. They also illustrate that spin splittings in altermagnets can exceed by an order of magnitude the record relativistic spin-orbit splittings in bulk crystals with heavy elements⁴⁸. Moreover, unlike the spin-orbit split bands, altermagnetism preserves a common $\mathbf{k}$ -independent spin quantization axis.

Finally, we emphasize that relativistic DFT calculations in RuO_2 and KRu_4O_8 , presented in Supplementary Sec. III,IV and Fig. S1,S2, show the expected weak effect of the spin-orbit coupling on the bands. This highlights that the apparent prominent features of the relativistic bands, including the spin-momentum locking characteristics and the electric crystal-field mechanism of the spin-splitting, still reflect the non-relativistic spin-group symmetries. In contrast, these prominent symmetries are omitted by the relativistic magnetic groups of RuO_2 and KRu_4O_8 . In general, as also illustrated in Sec. III,IV and Fig. S1,S2, only the spin-group formalism facilitates the sublattice coset decomposition into transformations which interchange atoms between same-spin and opposite-spin sublattices, which plays the central role in the understanding of altermagnetism.

Candidate materials

Tab. 1 lists selected candidate altermagnets. In Fig. 3 we highlight CrSb , a metal with the Néel temperature of 705 K⁴⁹. As shown in Fig. 3a, it crystallizes in the hexagonal NiAs -type structure (crystal space group $P6_3/mmc$)^{49,50}. The collinear antiparallel spin arrangement corresponds to the non-trivial spin Laue group $2_6/2_m2_m1_m$ ($[E \parallel \bar{3}m] + [C_2 \parallel C_{6z}][E \parallel \bar{3}m]$). It contains the $[C_2 \parallel M_z]$ symmetry, which makes the spin-momentum locking bulk-like. Additional mirror planes orthogonal to the three hexagonal crystal axes, combined with the spin rotation, imply that the spin winding number is $W = 4$. This is confirmed by the DFT

calculations in Fig. 3b.

CrSb has a more complex band structure than KRu_4O_8 , as shown in Fig. 3c. Nevertheless, we can still trace a pair of bands with opposite spin (highlighted by grey shading in Fig. 3c) which are degenerate at Γ , $\mathbf{L}_1$ and $\mathbf{L}_2$ points, and split when moving away from these high symmetry points. The spin splitting is as high as 1.2 eV. We also note that altermagnetic CrSb hosts an extraordinary spin-polarized quasiparticle which is four-fold degenerate at the Γ -point and spin split away from the Γ -point. In the Supplementary Sec. V and Figs. S3,S4 we discuss additional altermagnetic candidates among insulators, semiconductors and metals, and give an example illustrating the inversion symmetry of the altermagnetic bands even when the crystal is inversion asymmetric.

The variety of altermagnetic material types brings us back to the representative altermagnetic structure shown in Fig. 1. It corresponds to the parent cuprate La_2CuO_4 of a high-temperature superconductor⁵¹. The band structure for the collinear antiparallel spin arrangement on this crystal falls into the altermagnetic non-trivial spin Laue group $2_m2_m1_m$ ($[E \parallel 2/m] + [C_2 \parallel C_{2y}] [E \parallel 2/m]$). The symmetry element $[C_2 \parallel C_{2y}]$ generates a planar spin-momentum locking with a characteristic spin winding number $W = 2$. Remarkably, according to our spin-group theory, the energy bands of La_2CuO_4 are altermagnetically spin split. This is confirmed by the DFT calculations in Supplementary Fig. S5, and is in contrast with the conventional perception of spin-degenerate bands in La_2CuO_4 ⁵¹. The omission of the spin-splitting physics in earlier electronic-structure studies of cuprates could be explained by the focus on high-symmetry lines or planes, such as the $k_z = 0$ plane³⁶, where the states are spin-degenerate (see Supplementary Fig. S5). Our work thus brings a new element into the research of the coexistence and interplay of magnetic and superconducting quantum orders⁵².

Discussion

Our extraordinary spin-splitting mechanism by the local electric crystal-field in the Ru-oxide altermagnets provides a unifying microscopic picture of recent intriguing theoretical and experimental observations of spin-transport anomalies in the magnetically compensated RuO_2 , namely of the large spontaneous Hall, charge-spin conversion and spin-torque phenomena^{12,13,18,24,26–29}. We also note that our identification of altermagnetism in chalco-

genide CoNb_3S_6 , perovskite CaMnO_3 , or the cuprate La_2CuO_4 crystals sheds new light on puzzling magneto-transport anomalies found in literature on these materials^{53–55}.

The diversity of the altermagnetic material types illustrates the relevance of this magnetic phase for a range of condensed-matter physics fields. Apart from superconductors, unexplored connections might exist between altermagnetism and topological insulators and semimetals. In this context we note that, on one hand, symmetry prohibits a realization of altermagnetism in one-dimensional chains; collinear antiferromagnetic spin arrangements on one-dimensional chains have the $[C_2 \parallel \bar{E}]$ (and possibly also $[C_2 \parallel \mathbf{t}]$) symmetry and, therefore, have Kramers spin-degenerate bands. On the other hand, we have identified altermagnetic candidates among quasi-one-dimensional, quasi-two-dimensional, and three-dimensional insulators and metals. This opens the possibility of searching for unconventional spin-polarized fermion quasiparticles (cf. CrSb), topological-insulators and topological-semimetals, including Chern insulators with the quantized Hall effect in high-temperature systems with vanishing internal or external magnetic dipole.

We expect that the altermagnetic spin-momentum locking, with the extraordinary spin-splitting mechanism by the local electric crystal field, will play a special role in the search for new quantum phases, complementing the widely explored relativistic, magnetic, and many-body correlation physics. This applies to both basic science and technology contexts. Regarding the latter, our spin-group classification of spin-momentum locking for collinear spin arrangements, together with DFT calculations in representative crystals, theoretically underpins altermagnetism as a favourable magnetic phase for research and applications of charge-spin conversion devices, including magnetic memories. Among the candidate altermagnetic materials, we find high transition-temperature altermagnets composed of abundant light elements, which have a large energy separation of opposite spin states. Moreover, unlike ferromagnets, they eliminate stray fields and add insensitivity to external magnetic field perturbations. When comparing to the relativistic non-magnetic spin-texture phases, these share with altermagnets the zero net dipole-moment. However, large relativistic spin splittings require rare heavy elements. In addition, the relativistic phases suffer from spin decoherence even for small-angle elastic scattering off common isotropic impurities. We have illustrated that this obstacle is diminished in altermagnets by the collinearity of spins, and by the possibility of a large $\mathbf{k}$ -vector separation in the Brillouin zone of the equal-energy eigenstates with the opposite spin.

Phase Nontrivial spin Laue group (number of groups)	Ferromagnetism $\mathbf{R}_s^I = [E \parallel \mathbf{G}]$ (11)	Kramers antiferromagnetism $\mathbf{R}_s^{II} = [E \parallel \mathbf{G}] + [C_2 \parallel \mathbf{G}]$ (11)	Altermagnetism $\mathbf{R}_s^{III} = [E \parallel \mathbf{H}] + [C_2 \parallel \mathbf{G} - \mathbf{H}]$ (10)
Collinear spin arrangement on crystal Opposite spin-sublattice transformation	None	$[C_2 \parallel \bar{E}]$ or $[C_2 \parallel \mathbf{t}]$	$[C_2 \parallel A]$
Band structure		$[C_2 \parallel E]$	$[C_2 \parallel A]$

Fig. 1. **Illustration (in columns) of ferromagnetic, Kramers spin-degenerate antiferromagnetic, and altermagnetic phases.** **First row:** Non-trivial spin Laue group structure for the given magnetic phase with the number of different groups in brackets. **Second row:** Illustrative collinear spin arrangements on crystals. Opposite spin directions are depicted by purple and cyan color. Instead of marking the spin arrangement by arrows, we use a two-color representation to highlight that the overall spin axis orientation is not related to the real space coordinates for the non-relativistic spin-group symmetries. Ferromagnetic and Kramers antiferromagnetic crystals correspond to FeRh, the altermagnetic crystal to La_2CuO_4 . Red arrow and its label highlights opposite-spin-sublattice transformation symmetries which can generate Kramers spin-degenerate antiferromagnetism (real-space translation or inversion) and altermagnetism (real-space rotation). The collinear antiparallel spin arrangement in the altermagnet is further highlighted by the purple and cyan arrows next to the opposite spin sublattices. **Third row:** Band-structure cartoons show ferromagnetically spin-split bands (opposite spin states depicted by purple and cyan color), a Kramers spin-degenerate antiferromagnetic band, and altermagnetically spin-split bands. The opposite-spin-sublattice transformation of the spin Laue group which maps the same-energy eigenstates with opposite spins on the same $\mathbf{k}$ -vector in Kramers antiferromagnets and on different $\mathbf{k}$ -vectors in altermagnets is again highlighted.

Class-winding number		Spin-momentum locking	$\mathbf{G}$	$\mathbf{R}_s^{\text{III}}$	$\mathbf{H}$	$\mathbf{A}$	Candidate
Planar (k_x, k_y)	P-2	(k_x, k_y)	mmm	$2_m 2_m 1_m (8)$	$2/m$	C_{2x}	$\text{La}_2\text{CuO}_4, \text{FeSb}_2$
			$4/m$	$2_4/1_m (8)$		C_{4z}	KRu_4O_8
	P-4	(k_x, k_y)	$4/mmm$	$2_4/1_m 1_m 1_m (16)$	mmm	C_{4z}	$\text{RuO}_2, \text{MnO}_2, \text{MnF}_2$
				$1_4/1_m 2_m 2_m (16)$	$4/m$	C_{2x}	KMnF_3
	P-6	(k_x, k_y)	$6/mmm$	$1_6/1_m 2_m 2_m (24)$	$6/m$	C_{21}	
Bulk	B-2		$2/m$	$2_2/2_m (4)$	$\bar{1}$	C_2	CuF_2
	B-4		$\bar{3}m$	$1\bar{3}2_m (12)$	$\bar{3}$	C_{21}	$\text{CoF}_3, \text{FeF}_3, \text{Fe}_2\text{O}_3$
			$6/m$	$2_6/2_m (12)$		C_6	
	B-6		$6/mmm$	$2_6/2_m 2_m 1_m (24)$	$\bar{3}m$	C_6	$\text{CrSb}, \text{MnTe}, \text{VNb}_3\text{S}_6$
			$m\bar{3}m$	$1_m 1\bar{3}2_m (48)$	$m\bar{3}$	C_4	

Tab. I. **Classification of altermagnetic spin-momentum locking protected by spin-group symmetries, and material candidates.** The columns describe, respectively, planar (P) or bulk (B) spin-momentum locking with the corresponding spin winding number, the crystallographic Laue group $\mathbf{G}$, the halving subgroup $\mathbf{H}$ of symmetry elements which interchange atoms between same-spin sublattices, a generator $\mathbf{A}$ of symmetry elements which interchange atoms between opposite-spin sublattices, the non-trivial spin Laue group $\mathbf{R}_s^{\text{III}}$ (in the bracket we list the number of symmetry elements), and altermagnetic material candidates. The model $\mathbf{k} \cdot \mathbf{p}$ Hamiltonian bands on which we illustrate the spin-momentum locking character and spin winding number are described in Supplementary Sec. II. References describing the materials are in the main text and Supplementary Sec. III-V.

Fig. 2. Spin splitting by local electric crystal field in altermagnetic KRu_4O_8 . **a**, Schematic spin arrangement on the KRu_4O_8 crystal with opposite spin directions depicted by purple and cyan color. Red arrow and its label highlights the opposite-spin-sublattice transformation, containing a real-space four-fold rotation. **b**, Calculated spin-momentum locking with the spin winding number $W = 2$ on top of two DFT Fermi surface sheets. **c,d**, DFT band structure of the non-magnetic and altermagnetic phase, respectively. Grey shading highlights the $\mathbf{k}$ -dependent splitting by the local electric crystal field. **e,f**, Projection of bands on the sublattice A and B in the non-magnetic (black) and altermagnetic (purple and cyan) phase for the upper bands and lower bands, respectively. Color shading in panel f highlights the nearly $\mathbf{k}$ -independent magnetic splitting of the lower bands, and its opposite sign for the sublattice A and B bands. **g**, Real-space DFT spin density around the Ru atom in sublattice A and B.

Fig. 3. **Metallic high Néel temperature altermagnet CrSb.** **a**, Schematic crystal structure with DFT spin densities. Cr sublattices and the respective magnetization densities with opposite orientation of the magnetic moment are depicted by purple and cyan color. Red arrow and its label highlights the opposite-spin-sublattice transformation, containing a real-space mirror or six-fold rotation. **b**, Calculated spin-momentum locking with the bulk spin winding number $W = 4$ on top of two selected DFT Fermi surface sheets. **c**, DFT band structure in the altermagnetic phase. Wavevector dependence of the spin splitting between the bands highlighted by the grey shading is plotted in the lower panel.

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