

# Gloss and Modelling Studies of Stone Polishing, Using Linear Polishing Machines With Rotating Heads

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## Research Article

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# Abstract

The ornamental stone industry has always played an important role in the world economy, particularly in building construction. Polishing the slabs to increase its gloss, is an important processing operation to enhance the beauty and richness of these natural materials. Many industrial polishing machines rely on rotating heads movement along zigzag trajectories, eroding the surface as stochastically as possible, to avoid scratches and other visual defects caused by paths too symmetric. The displacement of the polishing head after a single zigzag movement and after a single rotation have been used to quantify the polishing process as these two parameters are related with the final stone gloss and are a measure of the efficiency of the polishing process. Applying experimental and new computer simulation techniques, we studied the influence of these two tool displacement parameters on the final stone gloss, and acquired insight into the accuracy of the simulation techniques that were applied here for the first time. We concluded that: 1) a clear correlation can be established between experimental and simulation data; 2) the two displacement parameters represent an effective way to control the quality and efficiency of the polishing process; 3) there is a limit for the gloss acquired through polishing processes, so polishing above a given threshold decreases the efficiency without increasing the quality.

## 1 Introduction

The commercial applications of ornamental stones have been progressively focusing on the surface aspect, so the study of the polishing parameters and development of the tools characteristics envisaging the improvement of the surface gloss have an increasing industrial importance, that must be paired with the scientific interest of understanding better the roughness and optical mechanisms that determine these surface phenomena.

Polishing is a finishing process aiming to achieve a high level of surface gloss, through the application of a sequence of abrasives (with decreasing grit sizes) [1–4]. Studying the output produced by the polishing heads (see Fig. 1) on the stone surface allows us to get insight into the influence of the various velocities controlling a linear polishing machine: the conveyor belt velocity,  $V_L$ , the cross velocity,  $V_T$ , and the rotational velocity,  $\omega$ . These studies were carried out measuring the surface gloss (as roughness measurements proved ineffective for the highly polished surfaces that were analysed), and comparing with computer simulations of the same polishing procedures, to better understand the geometrical and kinematic issues determining the final results.

## 2 Background

It has been shown [1, 5, 6] that the quality and efficiency of a stone polishing process in a linear polishing machine, with one or more rotating heads moving along zigzag trajectories, as indicated in Fig. 2, is controlled by a geometric condition relating the two linear velocities,  $V_L$  and  $V_T$ . This condition 1 states that after a complete zigzag movement (with two linear segments), the tool center should be closer to its

initial position than the tool diameter [1]:  $l < d$ , with  $d = 2r = \text{tool diameter}$ . Otherwise there will be gaps of size  $l - 2d$  where the polishing head does not interact with the surface.

In this work we suggest that a second condition should be taken into account, relating the linear and rotating tool speeds, thus including all the most relevant kinematic parameters involved in the process. This condition 2 states that after a complete rotation, the tool center should be closer to its initial position than the tool radius [5]:  $x < r$ . Otherwise each point of the surface only interacts with a small angular fraction of the circular polishing head, and in some circumstances it may not be touched at all.

The combination of these two conditions determines the relations that must exist between the three velocities involved in this polishing process: the conveyor belt velocity,  $V_L$ , the transverse head velocity,  $V_T$ , and the rotational head velocity,  $\omega$ .

Defining  $b$  as the width of the conveyor belt, the time needed for the tool to move across the belt is given by  $t_T = b/V_T$  and the belt shift after a zigzag becomes  $l = 2bV_L/V_T \leq d$  (limited by condition 1).

The distance  $x_S$  moved by the polishing head in one linear segment (half of a complete zigzag) is given by:

$$x_S = \sqrt{b^2 + \left(\frac{l}{2}\right)^2} = \sqrt{(V_T t_T)^2 + (V_L t_T)^2} = \frac{b}{V_T} \sqrt{V_T^2 + V_L^2} = b \sqrt{1 + (V_L/V_T)^2}$$

1

Defining  $n_S = \omega t_T$  as the number of rotations executed during the time  $t_T$  by the tool head rotating at  $\omega$  rotations per unit of time, the distance  $x$  that the tool head moves in a single rotation is given by (limited by condition 2):

$$x = \frac{x_S}{n_S} = \frac{b \sqrt{1 + (V_L/V_T)^2}}{\omega t_T} = \frac{V_T}{\omega} \sqrt{1 + (V_L/V_T)^2} \leq r$$

2

To assess the validity of condition 2 and its combination with condition 1, we acquired experimental data and compared with equivalent simulated results.

The polishing operations used in this work involved the last three stages of the polishing sequence (320, 400 and 5Extra grit sequence – see Fig. 3). This sequence was selected to achieve a mirrored surface, with a significant gloss.

a) b) c)

**Figure 3** : Sequence of abrasives of the polishing cycle used in this work: a) 320 grit; b) 400 grit; c) 5Extra grit

The quantitative effectiveness of the surface polishing was then assessed experimentally measuring the gloss with a gloss meter TCQ GL0030 (see Fig. 4), at 20°, 60° and 85° to the surface normal (the angles supported by the equipment). A wired grid positioned over the stone was used to define each square section where gloss was measured.

The light reflected (the gloss) for a given angle can be compared with a standard scale going from 100 gloss units (GU) for a highly reflecting black glass, to 0 gloss units for a perfectly matt surface [7]. Therefore, the measuring head of a gloss meter must be previously calibrated. Highly reflective materials such as mirrors may achieve gloss values as high as 1000, when measured at 20°. The measuring angle is selected according to the expected gloss: 1) 20° for high gloss, above 70 GU; 2) 60° for medium gloss, between 10 and 60 GU; 3) 85° for low gloss, below 10 GU. For example, when the gloss measured at 60° is above 70 GU, the measurement should be repeated at 20° to optimize precision [8].

To quantitatively assess the polishing results, roughness measurements were also tried, but surface fluctuations are too small for common roughness meters. Roughness measurements should be considered in tests involving much coarser surfaces where gloss is too small to be determined with standard equipment.

### 3 Computational Details

A few computer modelling studies have been previously reported [9, 10, 11] to analyse mechanical and chemical aspects related with the polishing process, but these studies do not aim to simulate the overall macroscopic result of a polishing treatment. To simulate the polishing process, we used PAM - Polishing Analysis Modelling, a new modelling tool developed to simulate the polishing processes occurring in the industry, namely in ornamental stone processing. Users are expected to supply information describing the polishing tools, the operational parameters and the trajectories to follow. In return PAM simulates the polishing process and returns graphic and statistical data allowing users to investigate the results and its causes.

This two-dimensional simulator moves and rotates a tool representation (see Fig. 5) over the stone surface, both represented by lattices of small cells (henceforth designated by pixels, typically with one mm of side), and accumulates the contacts between them (henceforth designated by abrasion) for each cell. The quality of the polished surface is analysed through a range of parameters that includes, for each pixel, the total abrasion, the x and y average polishing shifts (measured from the pixel to the tool center), the average distance and the distance standard deviation of the pixel (again, relatively to the tool center). Each contact of a surface cell (a pixel) with the polishing tool is accumulated giving the total abrasion. Abrasion can take any value from 0 (black cells) onward, with more white regions representing progressively more eroded cells. Fig. 6 represents the abrasion produced in two simulations of a tool with 320 grit elements, rotating at 600 rpm, for 100 and 1000 time steps per second, corresponding to increment angles of 36 and 3.6 degrees, respectively. Fig. 6a shows that, at this rotation speed, a time step of 0.01 sec is clearly insufficient to properly describe the fast movement of the tool over the stone.

Decreasing the time step to 0.001 s, as shown in Fig. 6b, the simulator is already able to account for the finer details of the movement, producing an essentially continuous pattern that seems to emulate well a real polishing tool rotating at high speed over a fixed stone.

a) b) c)

a) b)

**Figure 6** : Tool head with six 320 grit elements rotating at 10 rotations per second, simulated with: a) a time step of 0.01 s, corresponding to an increment angle of  $36^\circ$  per step; b) a time step of 0.001 s, corresponding to an increment angle of  $3.6^\circ$  per step.

The detailed data that can subsequently be acquired for more realistic simulations, involving complex paths, with straight and curved trajectories, with simultaneous translations and rotations, allow users to get detailed insight into the various aspects governing a stone polishing process.

The quality of the polished surface is analysed through a range of parameters that includes, for each pixel, the total abrasion, the x and y average polishing shifts (measured from the pixel to the tool center), the average distance and the distance standard deviation of the pixel (again, relatively to the tool center). Each contact of a surface cell (a pixel) with the polishing tool is accumulated giving the total abrasion. The detailed data thus acquired for each simulation allows users to get detailed insight into the various aspects governing a stone polishing process.

## 4 Experimental Procedure

During this work, we used a linear polishing machine with a single head, with a tool diameter  $d = 435$  mm and a cross distance on a transverse movement  $b = 240$  mm. We used constant values, previously optimised, for the conveyor belt speed  $V_L = 600$  mm/min, the head pressure  $P = 2$  bar, and the water flow  $Q = 30$  L/min. Six slabs of limestone, as equal as possible, were selected for these tests, due to the high homogeneity of its surface. This is required to simplify the comparison between experimental and simulation data, as the simulator assumes a perfect, two dimensions, stone surface. After applying the sequence of abrasives, the surface gloss is measured and compared with the abrasion predicted in the same conditions by the polishing simulator (see Fig. 7 and Fig. 8). To make the measurements more precise, we used a physical grid made of wire to define precisely the sections where gloss was measured to compare with simulated values. Throughout this work, sections with homogeneous simulated abrasion values were identified as green cells (see Fig. 7) while sections with simulated abrasion values too different were marked red and discarded in the subsequent analysis and comparison with experimental results.

To obey condition 1 ( $l < d$ ), with  $V_L = 600$  mm/min as stated above, the transverse speed  $V_T$  must be  $V_T \geq 20$  mm/s. To obey condition 2 ( $x < r$ ), with  $V_L = 600$  mm/min and  $V_T \geq 20$  mm/s, the head rotation speed must be  $\omega \geq 10$  rpm. Table 1 shows the various operational conditions tested in this work, whereas

l values are determined by condition 1 and  $\omega$  are determined by condition 2. Clearly, setting conditions 1 and 2 leads to an increase of the transverse velocity (to decrease l) and an increase of the rotational velocity (to decrease x). The simulated linear velocity (V) matches the vectorial combination of both cross and conveyor belt velocities from the polishing machine, according to equation:  $V = \sqrt{V_L^2 + V_T^2}$ .

The parameters used in the 6x4=24 simulations presented in Tab.1 aim to replicate the parameters used in the laboratory experiments. The 320, 400 and 5Extra grit abrasives used in this work (see Fig. 3) were simulated and replicated in order to generate the full polishing heads, with six abrasive elements each (see Fig. 5). The simulated stone has the real stone dimensions, assuming pixel cells with 1 mm x 1mm. The simulated tool paths were designed to emulate the real zigzag trajectories followed by the tool head.

Table 1  
24 polishing conditions used in experimental and modelling work, obeying conditions 1 and 2.

l (mm)	VT (mm/s)	V (mm/s)	$\omega$ (rpm)				
			x:	r	r/2	r/4	r/8
120	40	41.58		10	20	45	90
64	75	75.80		20	40	80	165
53	90	90.67		25	50	100	200
48	150	150.33		40	80	165	330
32	200	200.25		55	110	220	440
24	300	300.17		80	165	330	660

## 5 Results And Discussion

Given the typical conveyor belt speed used throughout this work ( $V_L = 600 \text{ mm/min} = 1 \text{ cm/s}$ ) and the relatively large tool head diameter ( $d = 435 \text{ mm}$ ), condition 1 is easily obeyed, even for small transverse speeds (see Tab.1). As expected, increasing the transverse speed requires larger rotational speeds, to fulfil condition 2. Decreasing x, from  $x = r$  to  $x = r/8$ , to further obey condition 2, requires even larger rotational speeds.

Experimental results (see Fig. 9) for surface gloss as a function of transverse velocity VT, for  $x = r$ ,  $x = r/2$ ,  $x = r/4$ ,  $x = r/8$  conditions, show a significant increase in gloss from 40 mm/s to 200 mm/s for all four x conditions. For higher transverse velocities, gloss remains essentially constant, showing that a maximum threshold has been attained and further increasing the energy spent in the polishing process (by increasing the transverse and rotational speeds) does not lead to a refinement of the surface quality.

The results clearly show that a better surface quality is obtained for smaller  $x$  values, when the rotating action is more effective. For  $x = r$ , the maximum attainable gloss is below 65 GU while for  $x = r/2$ ,  $x = r/4$ ,  $x = r/8$  the maximum gloss is above 70 GU, essentially the same value in the three cases. However, for  $x = r/8$  this limit is reached sooner, for lower transverse (and rotational) speeds.

Simulation results (see Fig. 10) for the same conditions show the same general trends, although the flat region for higher transverse velocities is not observed because the simulator simply adds abrasion contacts between the tool and the stone in a linear way, without considering any asymptotic effects.

Clearly gloss increases with transverse velocity, with a slope that essentially matches the values obtained from the experimental curves and the quality of the polished surface clearly increases from  $x = r$  to  $x = r/8$ . The curve for  $x = r/8$  was obtained from polished surfaces as those represented in Fig. 11, for three different transverse velocities, showing that as the zigzag trajectories become more parallel when the transverse velocity increases, the polishing intensity and surface homogeneity should also increase.

**Figure 11** : Abrasion images from polishing simulation, for three transverse velocities  $V_T$  : a) 40 mm/s; b) 90 mm/s; c) 200 mm/s, with  $x = r / 8$ .

Figure 12 compares experimental gloss with simulation abrasion, as a function of transverse velocity, for  $x = r/8$ . While the simulated abrasion increases linearly with transverse velocity, experimental gloss shows a less predictable evolution, although the overall trends are similar for both types of data. In both cases the polishing quality increases substantially when the transverse speed increases (and rotational speed, to obey condition 2).

However, the data in Fig. 9 and Table 1 clearly show that increasing separately these two speed parameters is not enough to achieve a good polished surface. Decreasing  $x$  from  $x = r$  to  $x = r/2$  is crucial to achieve a good polished surface. Decreasing  $x$  even further to  $x = r/8$  permits obtaining the same results at lower transverse speeds. In our case, working at  $x = r/8$  with  $V_T = 150\text{mm/s}$  ( $w = 330\text{rpm}$ , from Table1) provides essentially the same final quality (Fig. 10) as working at  $x = r/2$  with  $V_T = 200\text{mm/s}$  ( $w = 110\text{rpm}$ ). On the other hand, working at low  $V_T$  speeds such as 90 mm/s, a good polished surface is never attained, even for  $x = r/8$  and high rotational speeds ( $w = 200\text{rpm}$ ). Transverse and rotational speeds must be expertly combined to achieve adequate levels of polishing at low energy consumption.

## 6 Conclusions

In this set of experiments, we found that values for transverse velocities below 150 mm/s are insufficient to achieve the maximum surface quality and values above 250 mm/s are just wasting energy.

As expected in a linear polishing machine, the polishing quality increases with transverse and rotational velocities, until some maximum surface quality is achieved. Increasing even more the transverse or rotational velocities does not lead to further refinements in surface quality. Moreover, these two velocities must be expertly combined to get optimal results. Increasing independently the transverse or rotational

velocities does not necessarily lead to surfaces with maximum quality (industrial empirical evidence, shows that surface quality can even be reduced).

Conditions  $l < d$  and  $x < r$  must be applied to get the best results, thus providing mathematical relations between the three velocities (conveyor belt, transverse and rotational) involved in these processes.

These conclusions were sustained by both experimental and simulation results. Further experiments are required to confirm these conclusions, with other types of stone materials and linear polishing machines.

## **Declarations**

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### **b. Conflicts of Interest**

The authors have no relevant financial or non-financial interests to disclose.

The authors have no conflicts of interest to declare that are relevant to the content of this article.

### **c. Availability of data and material (data transparency)**

All data reported has been disclosed in the manuscript.

### **d. Code availability**

The research software used in the work is under development and, therefore, not available for general purpose yet.

### **e. Ethics approval**

Not applicable.

### **f.. Consent to participate**

All the authors agreed participating together in this work.

### **g.. Consent for publication**

All of the authors have read and agreed to publish this version of the manuscript.

### **h. Authors' contributions**

Adriano Coelho: conceptualization, investigation, experimental measurements and data collection; writing – reviewing

José Carlos Pereira: conceptualization, investigation, software development and data collection; writing – original draft, reviewing, editing and submission.

Pedro Amaral: methodology, investigation, funding acquisition and project management; writing – reviewing, editing and submission.

Luís Guerra Rosa: investigation and project management; writing – reviewing.

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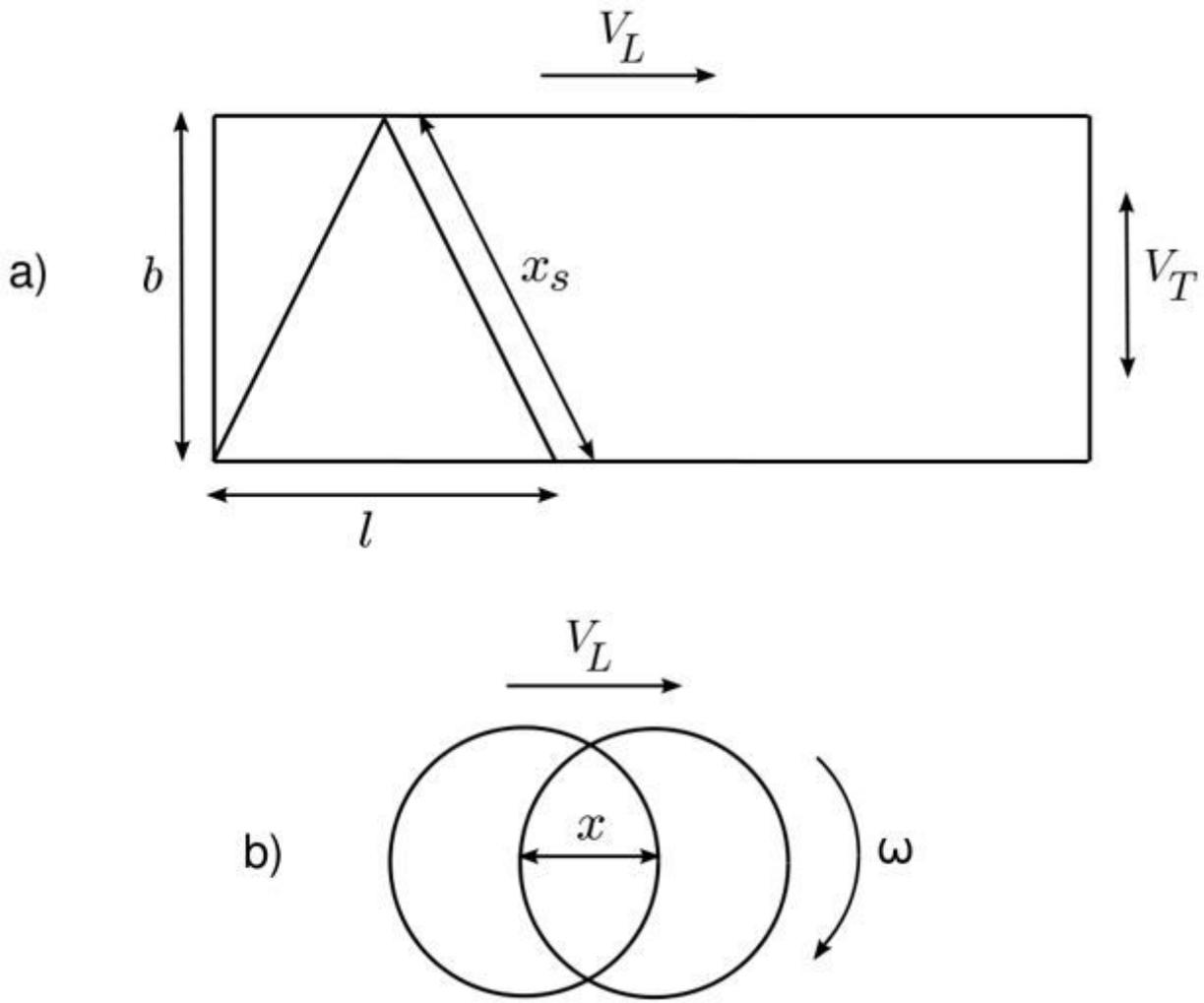
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## Figures



Figure 1

Linear polishing machines with rotating heads (example from PEDRINI).



**Figure 2**

The two polishing conditions. a)  $l \leq d$ ; b)  $x \leq r$ .



a)

b)

c)

Figure 3

Sequence of abrasives of the polishing cycle used in this work: a) 320 grit; b) 400 grit; c) 5Extra grit

### Glossmeter TQC GL0030

Base dimensions: 135 x 45 mm<sup>2</sup>  
Orifice size: 50 x 10 mm<sup>2</sup>  
Spot size: 20°: ± 5 x 5 mm<sup>2</sup>  
60°: ± 20 x 9 mm<sup>2</sup>  
85°: ± 30 x 9 mm<sup>2</sup>  
Resolution: 0,1GU (0-100GU)  
1GU (>100GU)



Measuring angle characteristics:

	20°	60°	85°
Range	0 -100 GU	0 -100 GU	0 -100 GU
Repeatability	0.4 GU	0.2 GU	0.2 GU
Reproducibility	1.69 GU	1.58 GU	1.88 GU
Bias	1.2 GU	0.6 GU	1.6 GU

Figure 4

Gloss meter TQC GL0030, used in this work.



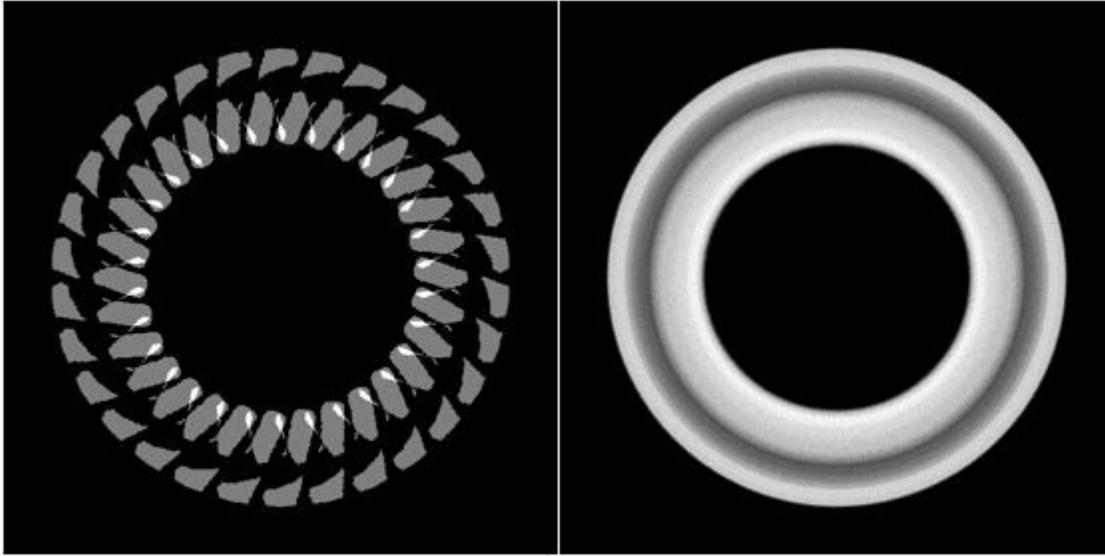
a)

b)

c)

Figure 5

Simulated tool heads used in this work, containing six abrasive elements of: a) 320 grit; b) 400 grit; c) 5Extra grit.

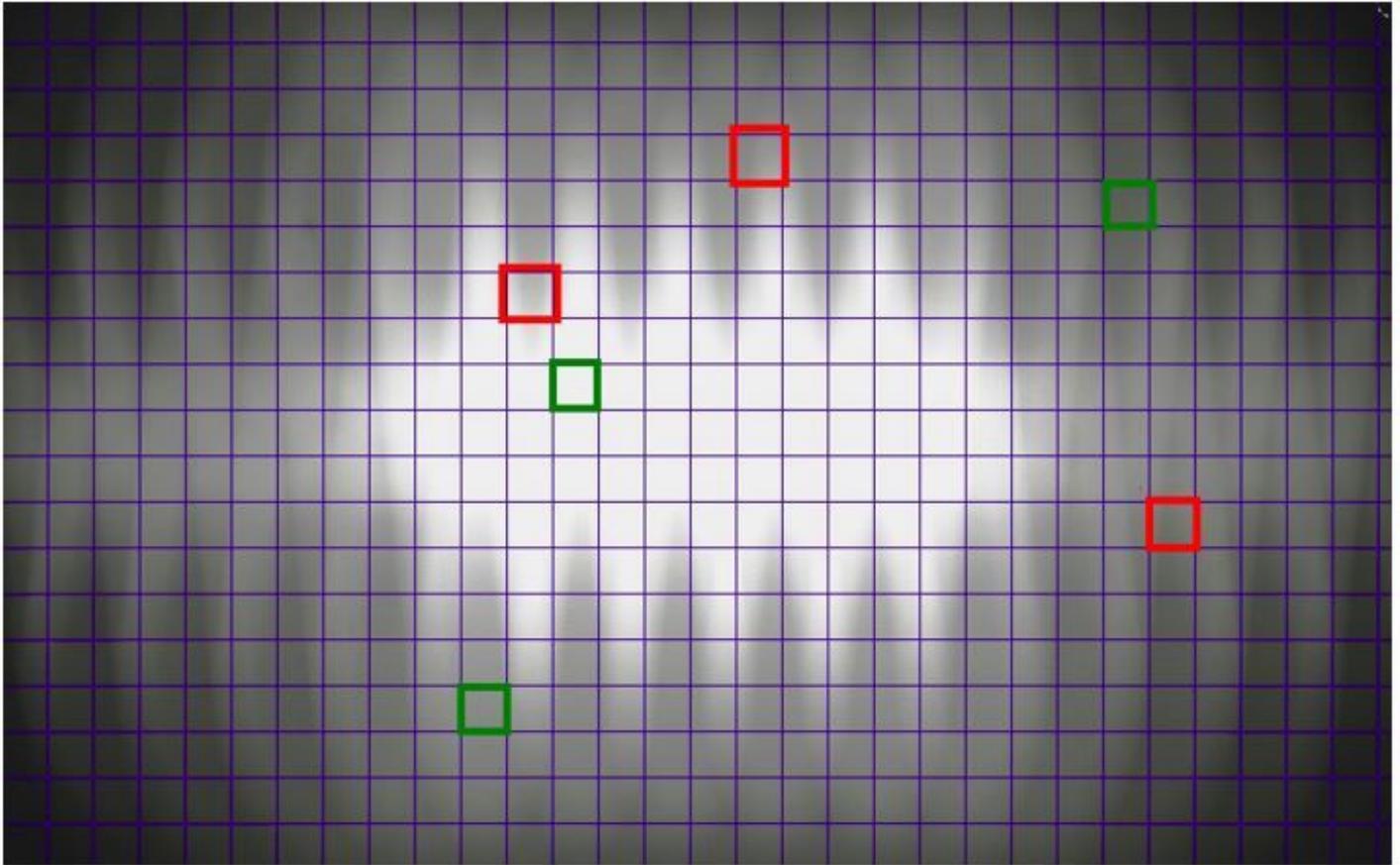


a)

b)

**Figure 6**

Tool head with six 320 grit elements rotating at 10 rotations per second, simulated with: a) a time step of 0.01 s, corresponding to an increment angle of  $360^\circ$  per step; b) a time step of 0.001 s, corresponding to an increment angle of  $3.60^\circ$  per step.



**Figure 7**

Output image showing the simulated abrasion with homogeneous (green) cells and heterogeneous (red) cells.

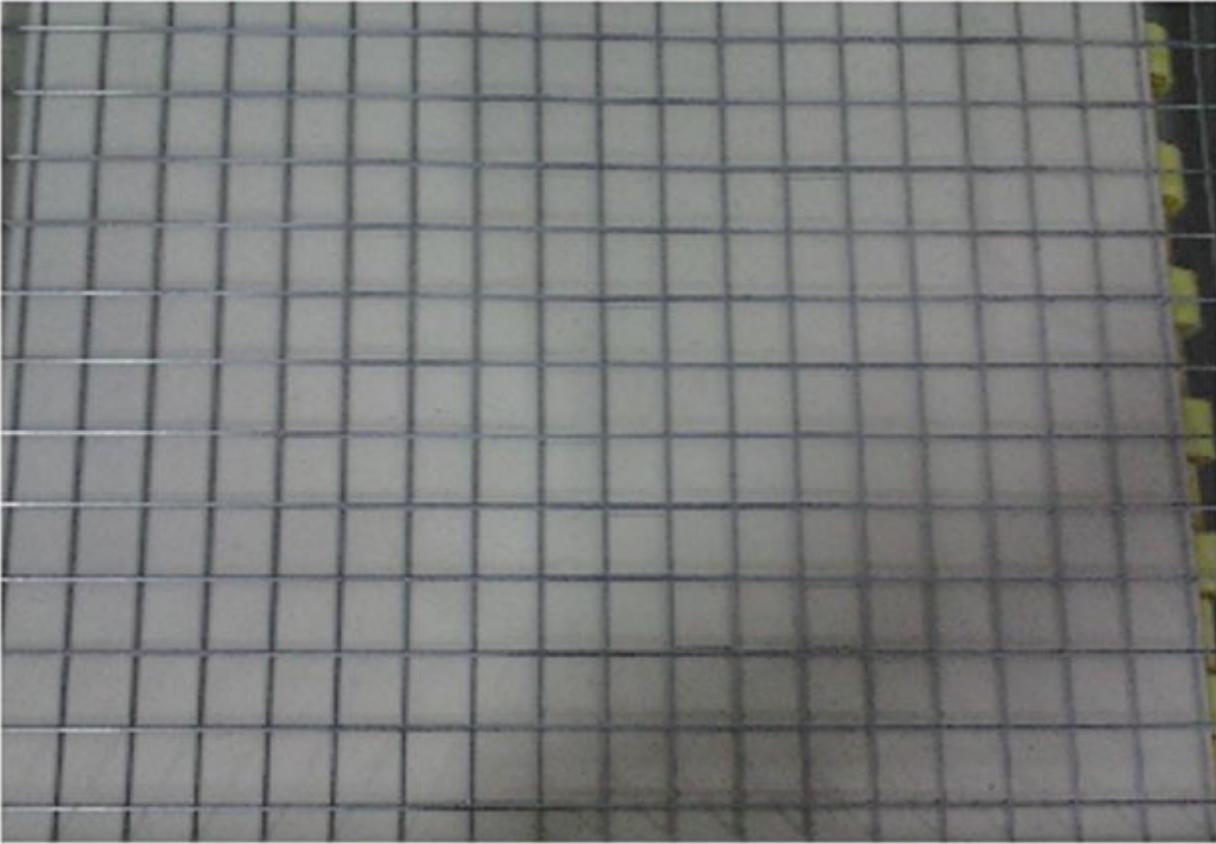


Figure 8

Experimental setup used to measure gloss data, using a wired grid with cells with  $30 \times 30 \text{ mm}^2$ , where each gloss measurement takes place.

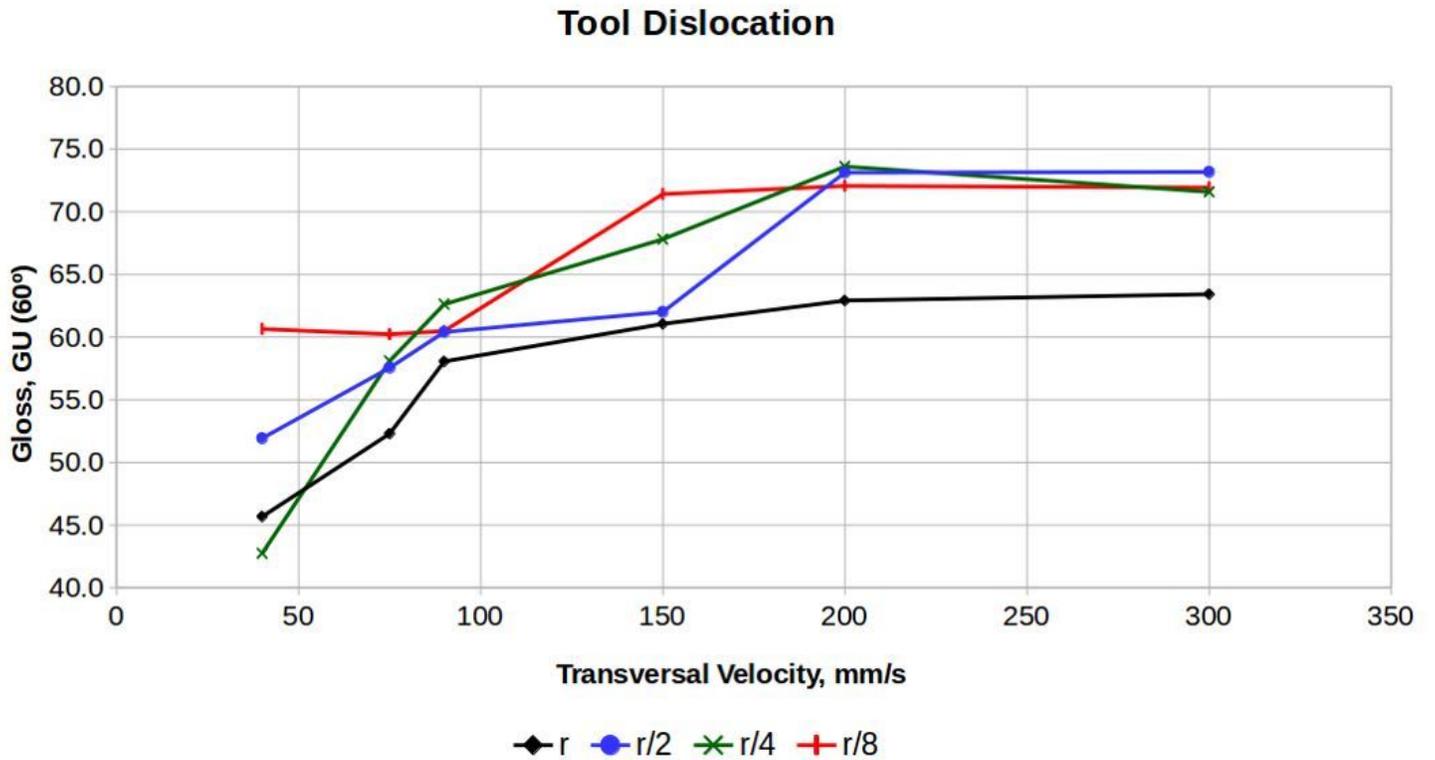


Figure 9

Gloss as a function of transverse velocity  $V_T$ , for  $x = r$ ,  $x = r/2$ ,  $x = r/4$  and  $x = r/8$ .

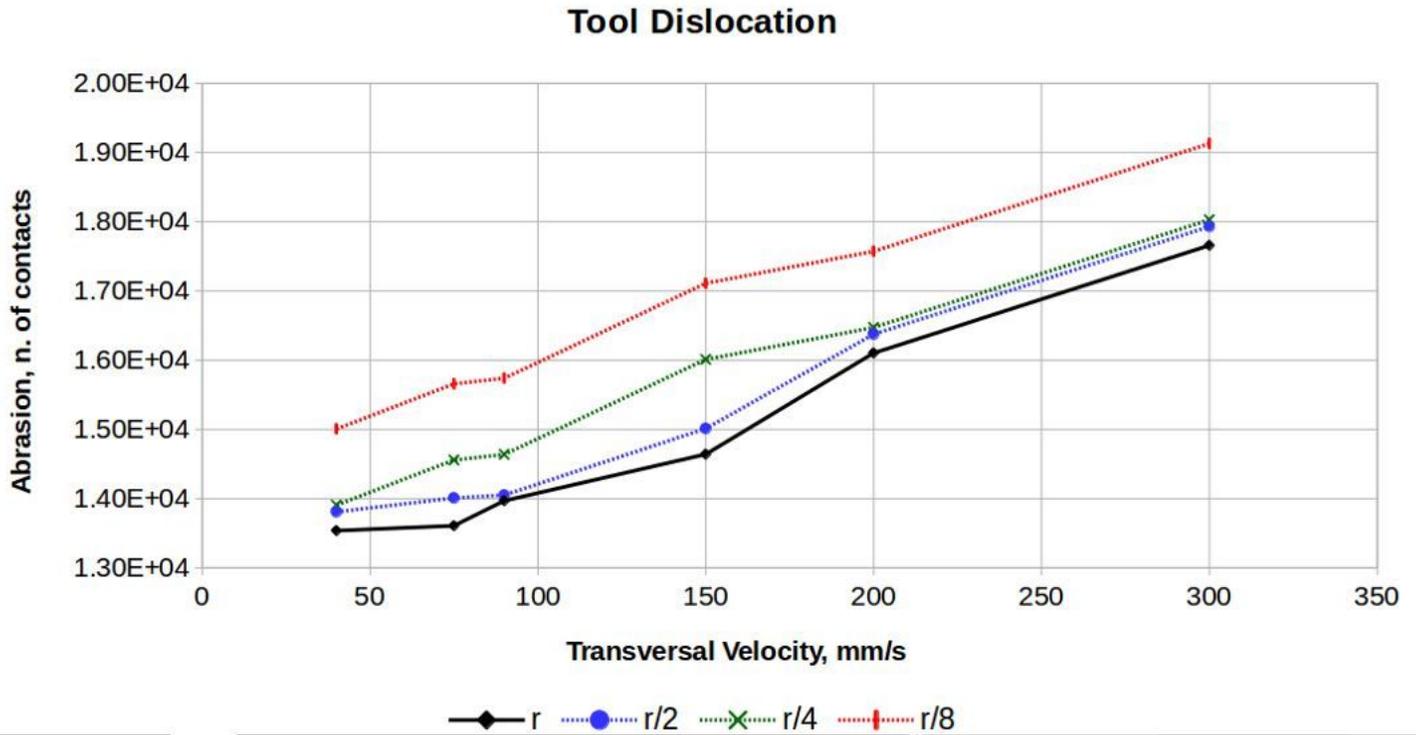


Figure 10

Abrasion as a function of transverse velocity  $V_T$ , for  $x = r$ ,  $x = r/2$ ,  $x = r/4$  and  $x = r/8$ .

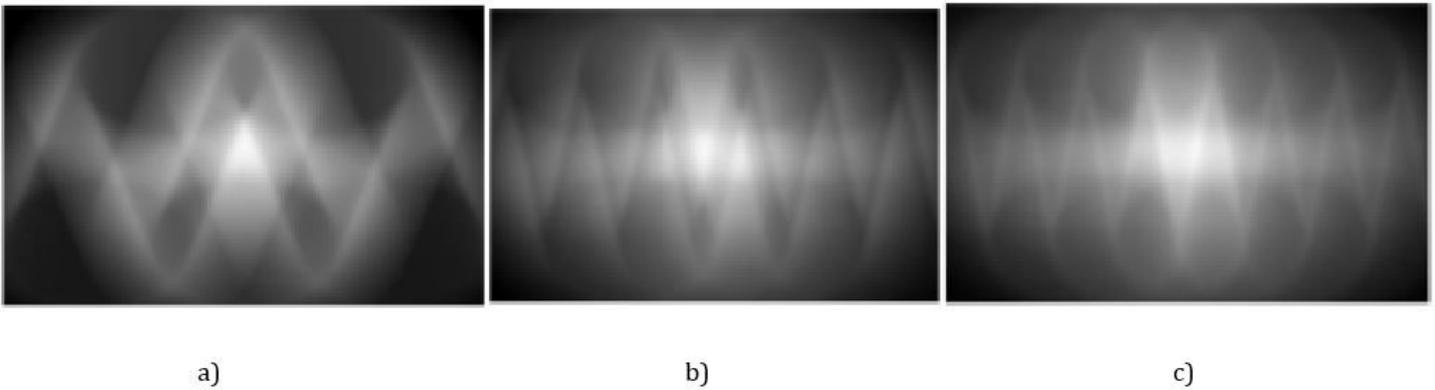


Figure 11

Abrasion images from polishing simulation, for three transverse velocities  $V_T$ : a) 40 mm/s; b) 90 mm/s; c) 200 mm/s, with  $x = r / 8$ .

## Tool Dislocation

$$x = r / 8$$

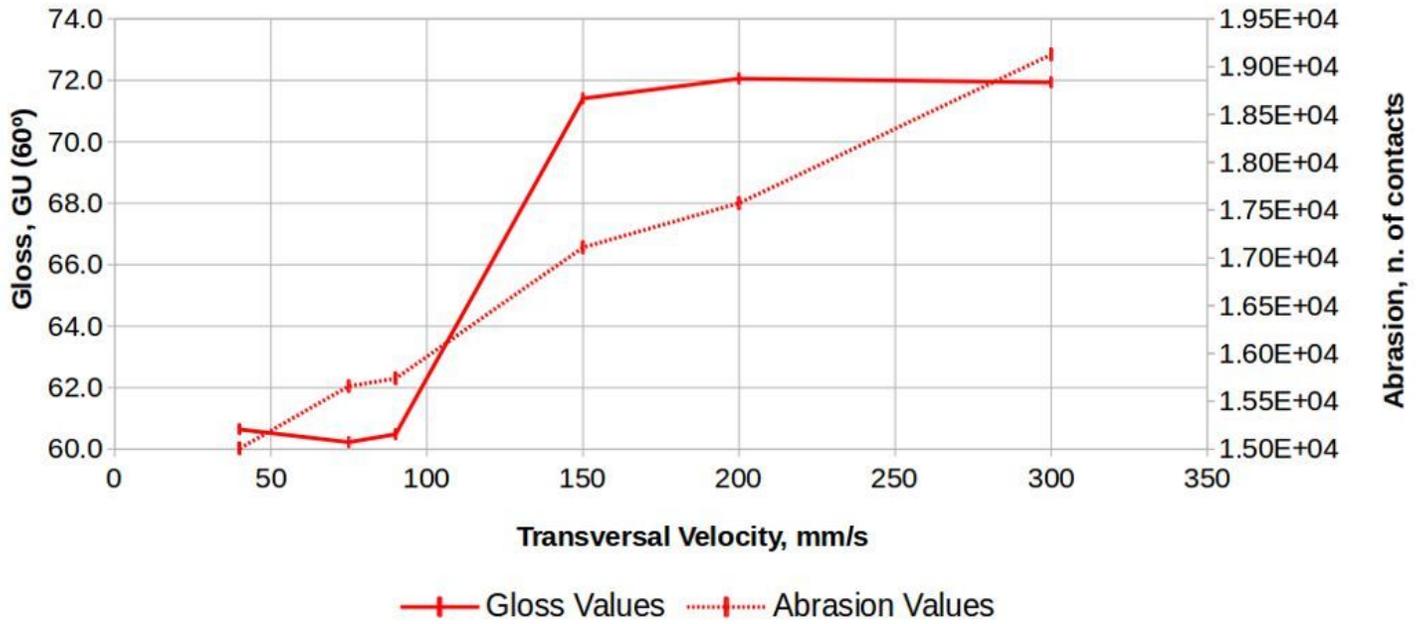


Figure 12

Comparison of abrasion and gloss results, both as in function of transverse velocity  $V_T$ , for  $x = r/8$ .